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Drift-Compensated Low-Noise Frequency Synthesis Based on a cryoCSO for the KRISS-F1

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Abstract — In this paper, we report on the implementation and stability analysis of a drift-compensated frequency synthesizer from a cryogenic sapphire oscillator (CSO) designed for a Cs/Rb atomic fountain clock. The synthesizer has two microwave outputs of 7 and 9 GHz for Rb and Cs atom interrogation, respectively. The short-term stability of these microwave signals, measured using an optical frequency comb locked to an ultrastable laser, is better than $5 \times 10^{-15}$ at an averaging time of 1 s. We demonstrate that the short-term stability of the synthesizer is lower than the quantum projection noise limit of the Cs fountain clock, KRISS-F1(Cs) by measuring the short-term stability of the fountain with varying trapped atom number. The stability of the atomic fountain at 1 s averaging time reaches $2.5 \times 10^{-14}$ at the highest atom number in the experiment when the synthesizer is used as an interrogation oscillator of the fountain. In order to compensate the frequency drift of the CSO, the output frequency of a waveform generator, in the synthesis chain, is ramped linearly. By doing this, the frequency stability of the synthesizer at an average time of one hour reaches a level of $10^{-16}$, which is measured with the fountain clock.

Index Terms — Cryogenic sapphire oscillator (CSO), frequency stability, frequency synthesizer, hydrogen maser, optical frequency comb, quantum projection noise (QPN), stable lasers.

I. INTRODUCTION

The most accurate realization of the international system of units now has been made by the atomic fountain frequency standards, some of which reached an uncertainty at a level of $10^{-16}$ [1]–[5]. To this end, an interrogation oscillator, a microwave signal for the interrogation of the atomic resonance, needs to meet stability requirements at both short and long measurement time. Good short-term stability is essential to reduce the effect of the phase noise of the local oscillator on the pulsed operation of the clock [6], [7] and allows fountain clocks to operate in the quantum projection noise (QPN) limited regime [8], which is at a level of about $10^{-14}$ for $10^8$ atoms. In addition, better short-term stability greatly facilitates the accuracy evaluation by dramatically shortening the time needed to reach the target stability. Long-term frequency stability at a level of a few parts in $10^{-16}$ or better is necessary to reach the target uncertainty of $10^{-16}$.

As an interrogation oscillator for the Cs atomic fountain clock in the Korea Research Institute of Standards and Science, KRISS-F1(Cs), we used a hydrogen maser (H-maser) filtered by a low-noise BVA quartz oscillator. This approach meets the long-term stability requirements but limits the short-term stability of the fountain clock to about $1 \times 10^{-13}$ at 1 s averaging time, dominated by the phase noise of the interrogation oscillator. Recently, we introduced a cryogenic sapphire oscillator (CSO) using an ultralow vibration pulse-tube cryocooler (cryoCSO) developed by Hartnett’s group [9]. The stability of this cryoCSO was measured using another cryoCSO before shipment to the KRISS laboratory, as described in [10] (curve 4 in Fig. 6). The short-term stability of the cryoCSO was measured to be as low as $2 \times 10^{-15}$ at 1 s averaging time with a long-term frequency drift of about $5 \times 10^{-14}$/day. The output frequency is at 11.200044 GHz, so we designed a stable frequency synthesizer for the fountain clock as briefly described in [11]. The short-term stability of its microwave output signals, which was measured by comparison with an ultrastable laser via an optical frequency comb, is better than $5 \times 10^{-15}$ over an averaging time of 1 s. We confirmed that the short-term stability of the KRISS-F1(Cs) operating with this synthesizer is QPN limited for a wide range of atoms. The long-term frequency drift is usually compensated by a loose phase-lock to an H-maser with a large time constant ($\sim 1000$ s) [3], [12]–[18]. In this paper, since this drift is almost linear, we canceled the linear frequency drift by applying a linear frequency ramp to the synthesizer. With this passive compensation, the long-term frequency stability reached $4 \times 10^{-16}$ at a day.

II. DESIGN OF THE FREQUENCY SYNTHESIZER

We built a frequency synthesizer with the cryoCSO as shown in Fig. 1. The output frequency of the cryoCSO is about 11.200044 GHz. The frequency drift of the cryoCSO was...
µWG (1 linear drift rate is too small to be compensated with a single shown in the shaded gray region in Fig. 1. Because the mixer [19] and two digital waveform generators (WGs) as frequency 44 kHz was removed using an in-phase/quadrature (IQ)
mixer [19] and two digital waveform generators (WGs) as shown in the shaded gray region in Fig. 1. Because the linear drift rate is too small to be compensated with a single WG (1 µHz frequency resolution), two WGs were used. We could compensate the linear drift by ramping 10-MHz output frequency from another WG (WG2) which is used as the reference frequency for the WG1. The ramping rate should be $1.4 \times 10^{-12}/s = 6.2$ nHz/s/44 kHz, so we changed the output frequency 10 MHz from WG2 is remotely controlled, so that it is ramped linearly. Details are described in the text.

The synthesized microwave signals have a short-term stability is not dominated by the noise of the interrogation oscillator, but instead by QPN.

### A. Measurement With the Stable Optical Clock Laser

We have developed an ultrastable 578-nm clock laser for an Yb optical lattice clock [21]. It is locked to a high-finesse optical cavity, made of ultralow thermal expansion glass. Its frequency stability [Allan deviation (ADEV)] can be measured either by comparison with another independent clock laser or by direct measurement using Yb atoms in the optical lattice. Its short-term stability is about $2 \times 10^{-15}$ for 1 s averaging time.

Fig. 2 describes the measurement setup. To compare the optical laser frequency with a microwave signal, we used an erbium-doped fiber frequency comb (FC1500, Menlo systems) centered at 1550 nm with a repetition rate of 250 MHz. We transferred the stability of the clock laser into the microwave frequency region using high-bandwidth ($\sim 300$ kHz) phase-locking of the frequency comb to the clock laser with a built-in electro-optic modulator, along with the carrier-envelope offset frequency ($\delta_{CEO}$) control using feedback to the pump laser current. The out-coupled comb is amplified and fed into a low-noise photodetector (DSC50S, Discovery). Its output signal is mixed with the output signals of the synthesizer or the cryoCSO. By doing this, the down-converted outputs of the synthesizer can be used for stability measurements using the phase detector (5125A phase-noise test set, Microsemi), which has an input frequency range from 1 to 400 MHz. The repetition rate $f_{rep}$ is adjusted to 249.775 MHz, so the down-converted frequencies of 7, 9, and 11 GHz are 6.3, 8.1, and 210 MHz, respectively.

Before making stability measurements using the setup in Fig. 2, we first needed to verify that the 100-MHz reference to the 5125A test set has sufficiently low noise to measure the stability of the microwave signals at the level of $10^{-15}$ or below. Because the microwave signals are down-converted by three orders of magnitude, the stability of the 100-MHz reference needs only to be below $10^{-12}$. This was verified by comparison with 250-MHz output from the comb. Fig. 3 (inset) shows that the instability of the 100-MHz signal is below $10^{-14}$ up to 100 s of averaging.

Fig. 3 shows the stability for the 7 and 9 GHz signals from the cryoCSO and that of the 11.2-GHz signal from the cryoCSO. It is noted that these are the combined stability of microwave signals generated both from the frequency comb and the synthesizer. The stability of the 11.2-GHz output directly from the cryoCSO is $4 \times 10^{-15}$ at 1 s, which is worse than that determined by Hartnett’s group using another cryoCSO [see Fig. 3 (dashed line)]. This means that the short-term stability measurement is limited by the transferred stability of the frequency comb from the clock laser. Besides the electronic noise from the photodetector, we infer that our fiber frequency comb itself contributes to the instability from the fact that the measured stability at 1 s of $\delta_{CEO}$ is at the level of 1 Hz, which corresponds to $4 \times 10^{-15}$ against 259 THz (half the clock laser frequency).

From the results of the stability measurements, we conclude that the synthesized microwave signals have a short-term
HEO et al.: DRIFT-COMPENSATED LOW-NOISE FREQUENCY SYNTHESIS BASED ON A cryoCSO FOR THE KRISS-F1

Fig. 2. Setup for the short-term stability measurements. Output signals from the synthesizer and the cryoCSO are down-converted by mixing with filtered beat signals from the frequency comb which is locked to the optical reference. The frequency stability of down-converted signals was measured using a phase detector, a Microsemi 5125A phase noise test set, which outputs phase difference data in units of cycles of the input signal. We used the 100-MHz signal from the synthesizer as a reference.

Fig. 3. Fractional frequency stability of the output signals from the synthesizer and the cryoCSO. The noise equivalent bandwidth of the phase detector (5125A) is set to 0.5 Hz. ADEV is computed from the phase difference data. The frequency drift after 10 s comes from that of the clock laser whose drift is depicted in the gray solid line. The dashed line shows the stability measurement using another cryoCSO. Small error bars are not visible. The inset is the stability of 100 MHz from the synthesizer.

stability of $\sim 5 \times 10^{-15}$ at 1 s, which is sufficient to be used for an atomic fountain clock, and the stability of the output signals from the synthesizer is not degraded by more than a factor of three in comparison with that of the cryoCSO, assuming it still has the same frequency stability measured by Hartnett’s group as shown by Fig. 3 (dashed line).

B. QPN-Limited Operation of the Atomic Fountain Clock

Since the short-term stability of the synthesized microwave signals is below $10^{-14}$, we can expect that an atomic fountain clock will operate in the QPN limit when these microwave signals are used as an interrogation oscillator [22].

Fig. 4 shows the frequency synthesis chain of an interrogation oscillator for the KRISS-F1(Cs). The 9-GHz and 100-MHz output of the cryoCSO synthesizer are mixed with each other to make the 9.1-GHz microwave. The 9.1-GHz microwave signal is mixed again with a 92.63177-MHz output of a direct digital synthesizer (DDS), which is referenced to the 800-MHz signal from the cryoCSO synthesizer. To avoid aliasing in the DDS, the 800-MHz signal is used as the reference frequency of the DDS so that the Nyquist frequency of the DDS is much higher than the output frequency of about 92 MHz. Finally, the synthesized microwave of 9.19263177 GHz is sent to the atomic fountain. For pulsed microwave operation in the fountain, an interferometer switch [23] is used. The microwave signal delivered to the fountain is switched by switching the 100-MHz signal as shown in Fig. 4. The frequency of the microwave sent to the fountain for Ramsey interrogation is tuned by controlling the DDS output frequency.

To confirm that the stability of the microwave signal is better than the QPN limit in the fountain, the short-term stability of the fountain was measured with varying the trapped atom number as shown in Fig. 5. In the QPN limit, the stability at 1 s averaging time improves with increasing number of detected atoms [8] satisfying the following relation:

$$\sigma(\tau = 1 s) \propto N^{-1/2},$$

where $N$ is the number of detected atoms. Fig. 5 shows that the dependence of the stability on the number of detected atoms is in good agreement with (1). This result shows that the short-term stability of the fountain is not affected by the stability of the output signals from the synthesizer. Therefore, we confirm that the short-term stability of the synthesized microwave signal is better than the QPN limit of our atomic fountain. Fig. 5 shows that the frequency stability improves to $2.5 \times 10^{-14}$ for the highest number of detected atoms.

IV. LONG-TERM STABILITY AND DRIFT COMPENSATION

The long-term stability of the synthesizer was measured by comparing the synthesized 9 GHz with the KRISS-F1(Cs)
Fig. 4. Block diagram for the local oscillator for KRISS-F1(Cs) from the 9-GHz synthesizer output. Its pulsed operation is carried out by switching 100 MHz before the first mixer. Mixers are single-sideband mixers to suppress the unwanted carrier signals.

Fig. 5. Short-term stability measured by the KRISS-F1(Cs) with varying trapped atom number [11]. Dashed line is the fit according to (1). The horizontal axis represents the magnitude of the time-of-flight signal which is proportional to the number of atoms.

using the setup described in Fig. 4. The synthesizer has a linear frequency drift of $4.8 \times 10^{-14}$/day coming from the cryoCSO (curve 1 in Fig. 6). This drift can make it difficult to carry out some of the essential measurements for the accuracy evaluation of the fountain clock if they take longer than a few thousands of seconds to reach targeted uncertainty, because the drift takes effect after 1 h as seen in curve 1 in Fig. 6. One example of these measurements is the evaluation of the sensitivity of the distributed cavity phase shift, which demands interleaved measurements for various mechanical tilts of the fountain clock [24]. In the case of successive adjustments of two different tilts, total duration of measurements for a single tilt should be less than half an hour. This is challenging because we need to mechanically change the tilt every half an hour or less. Because the frequency drift has been quite linear, we decided to compensate passively the linear part of the drift within the frequency synthesizer setup as shown in Fig. 1, instead of active phase-locking to an H-maser.

Fig. 6 shows the frequency stability of the synthesized 9-GHz signal measured by comparing it with the KRISS-F1(Cs), and that of the cryoCSO itself measured with another cryoCSO by Hartnett’s group before being shipped to our laboratory. As seen in curves 1–3 in Fig. 6, the stability up to 1000 s is governed by the stability of the KRISS-F1(Cs). After 1000 s, the frequency drift from the cryoCSO becomes dominant. This drift measurement agrees well with the measurement made using another cryoCSO (curve 4 in Fig. 6). We first tried compensation by ramping the frequency of the WG2 in Fig. 1 by 1 μHz frequency steps every 710 ms estimated from curve 1. From curve 2, it was found that there still existed the linear frequency drift due to an error in the estimation of the time interval from curve 1. So, we adjusted the interval by about 50 ms. After the second compensation, the long-term-stability of the fountain clock reached a level of $7 \times 10^{-16}$ within an hour.

V. CONCLUSION

We designed and implemented a frequency synthesizer using a cryoCSO for use as an ultrastable interrogation oscillator of a Cs/Rb atomic fountain clock. The short-term stability of the microwave signals from the synthesizer was about $5 \times 10^{-15}$ at 1 s of averaging. With this ultralow-noise microwave local oscillator, we have demonstrated the QPN-limited operation of our Cs fountain.
clock. KRIS-F1(Cs). From this result, we are assured that the short-term stability of the microwave synthesizer is below the QPN limit of our fountain. For the accuracy evaluation of the fountain with $10^{-16}$ uncertainty level, the long-term frequency drift of the cryoCSO was compensated by adjusting an offset frequency from a WG deployed in the synthesizer. The resultant long-term stability of the synthesized microwave signals, as measured by the fountain clock, approach a level of a few parts in $10^{-16}$.

REFERENCES


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