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Nucleon form factors and a nonpointlike diquark

J. C. R. Bloch,¹ C. D. Roberts,¹ S. M. Schmidt,¹ A. Bender,² and M. R. Frank³

¹*Physics Division, Building 203, Argonne National Laboratory, Argonne, Illinois 60439-4843*

²*Centre for the Subatomic Structure of Matter, University of Adelaide, Adelaide SA 5005, Australia*

³*Institute for Nuclear Theory, University of Washington, Seattle, Washington 98195*

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Nucleon form factors are calculated on $q^2 \in [0,3]$ GeV² using an ansatz for the nucleon's Faddeev amplitude motivated by quark-diquark solutions of the relativistic Faddeev equation. Only the scalar diquark is retained, and it and the quark are confined. A good description of the data requires a, nonpointlike diquark correlation with an electromagnetic radius of $0.8 r_\pi$. The composite, nonpointlike nature of the diquark is crucial. It provides for diquark-breakup terms that are of greater importance than the diquark photon absorption contribution. [S0556-2813(99)51711-1]

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Mesons present a two-body problem, and the Dyson-Schwinger equations (DSEs) have been widely used in the calculation of their properties and interactions [1,2]. Many studies have focused on electromagnetic processes, such as the form factors of light pseudoscalar [3,4] and vector mesons [5], and the $\gamma^* \pi^0 \rightarrow \gamma$ [6–8], $\gamma^* \pi \rightarrow \rho$ [7], and $\gamma \pi^* \rightarrow \pi \pi$ [9] transition form factors, all of which are accessible at the Thomas Jefferson National Accelerator Facility. These studies provide a foundation for the exploration of nucleons, which is fundamentally a three-body problem.

The nucleon's bound state amplitude can be obtained from a relativistic Faddeev equation [10]. Its analysis may be simplified by using the feature that ladderlike dressed-gluon exchange between quarks is attractive in the color antitriplet channel. Then, in what is an analogue of the rainbow-ladder truncation for mesons, the Faddeev equation can be reduced to a sum of three coupled equations, in which the primary dynamical content is dressed-gluon exchange generating a correlation between two quarks and the iterated exchange of roles between the dormant and diquark-participant quarks. Following this approach, the diquark correlation is represented by the solution of a homogeneous Bethe-Salpeter equation in the dressed-ladder truncation and hence its contribution to the quark-quark scattering matrix, \mathcal{M}_{qq} , is that of an asymptotic bound state; i.e., it contributes a simple pole. That is an artifact of the ladder truncation [11] and complicates solving the Faddeev equation [12] by introducing spurious free-particle singularities in the kernel.

Studies of DSE models [1,2] suggest that confinement can be realized via the absence of a Lehmann representation for colored Green's functions, and have led to a phenomenologically efficacious parametrization of the dressed-quark Schwinger function [3]. A similar parametrization of the diquark contribution to \mathcal{M}_{qq} , advocated in Ref. [13], has been used to good effect in solving the Faddeev equation [14]. We use such representations herein.

The nucleon-photon current is¹

$$J_\mu(P', P) = ie \bar{u}(P') \Lambda_\mu(q, P) u(P), \quad (1)$$

where the spinors satisfy $\gamma \cdot P u(P) = i M u(P)$, $\bar{u}(P) \gamma \cdot P = i M \bar{u}(P)$, with $M = 0.94$ GeV the nucleon mass, and $q = (P' - P)$. The complete specification of a fermion-vector-boson vertex requires 12 independent scalar functions:

$$\begin{aligned} i \Lambda_\mu(q, P) = & i \gamma_\mu f_1 + i \sigma_{\mu\nu} q_\nu f_2 + R_\mu f_3 + i \gamma \cdot R R_\mu f_4 \\ & + i \sigma_{\nu\rho} R_\mu q_\nu R_\rho f_5 + i \gamma_5 \gamma_\nu \epsilon_{\mu\nu\rho\sigma} q_\rho R_\sigma f_6 + \dots, \end{aligned} \quad (2)$$

where $f_i = f_i(q^2, q \cdot P, P^2)$, $R = (P' + P)$, and $q \cdot R = 0$ for elastic scattering. However, using the definition of the nucleon spinors, Eq. (1) can be written

$$J_\mu(P', P) = ie \bar{u}(P') \left(\gamma_\mu F_1(q^2) + \frac{1}{2M} \sigma_{\mu\nu} q_\nu F_2(q^2) \right) u(P), \quad (3)$$

where the Dirac and Pauli form factors are

$$F_1 = f_1 + 2M f_3 - 4M^2 f_4 - 2M q^2 f_5 - q^2 f_6, \quad (4)$$

$$F_2 = 2M f_2 - 2M f_3 + 4M^2 f_4 + 2M f_5 - 4M^2 f_6, \quad (5)$$

in terms of which one has the electric and magnetic form factors:

$$G_E(q^2) = F_1(q^2) - \frac{q^2}{4M^2} F_2(q^2), \quad (6)$$

$$G_M(q^2) = F_1(q^2) + F_2(q^2). \quad (7)$$

To calculate these form factors we represent the nucleon as a three-quark bound state involving a diquark correlation, and require the photon to probe the diquark's internal structure. Antisymmetrization ensures there is an exchange of roles between the dormant and diquark-participant quarks and this gives rise to diquark "breakup" contributions. We describe the propagation of the dressed-quarks and diquark correlation by confining parametrizations and hence pinch singularities associated with quark production thresholds are absent. Our calculation is related to many studies of meson properties [3–7,9].

¹In our Euclidean formulation, $p \cdot q = \sum_{i=1}^4 p_i q_i$, $\{\gamma_\mu, \gamma_\nu\} = 2 \delta_{\mu\nu}$, $\gamma_\mu^\dagger = \gamma_\mu$, $\sigma_{\mu\nu} = i/2 [\gamma_\mu, \gamma_\nu]$, and $\text{tr}_D [\gamma_5 \gamma_\mu \gamma_\nu \gamma_\rho \gamma_\sigma] = -4 \epsilon_{\mu\nu\rho\sigma}$, $\epsilon_{1234} = 1$.

We write the Faddeev amplitude of the nucleon as [15]

$$\begin{aligned} \Psi_{\alpha}^{\tau}(p_1, \alpha_1, \tau^1; p_2, \alpha_2, \tau^2; p_3, \alpha_3, \tau^3) \\ = \varepsilon_{c_1 c_2 c_3} \delta^{\tau \tau^3} \delta_{\alpha \alpha_3} \psi(p_1 + p_2, p_3) \Delta(p_1 + p_2) \\ \times \Gamma_{\alpha_1 \alpha_2}^{\tau^1 \tau^2}(p_1, p_2), \end{aligned} \quad (8)$$

where $\varepsilon_{c_1 c_2 c_3}$ effects a singlet coupling of the quarks' color indices, (p_i, α_i, τ^i) denote the momentum and the Dirac and isospin indices for the i th quark constituent, α and τ are these indices for the nucleon itself, $\psi(l_1, l_2)$ is a Bethe-Salpeter-like amplitude characterizing the relative-momentum dependence of the correlation between diquark and quark, $\Delta(K)$ describes the propagation characteristics of the diquark, and

$$\Gamma_{\alpha_1 \alpha_2}^{\tau^1 \tau^2}(p_1, p_2) = (C i \gamma_5)_{\alpha_1 \alpha_2} (i \tau_2)^{\tau^1 \tau^2} \Gamma(p_1, p_2) \quad (9)$$

represents the momentum-dependence, and spin and isospin character of the diquark correlation; i.e., it corresponds to a diquark Bethe-Salpeter amplitude.

With this form of Ψ , we retain in \mathcal{M}_{qq} only the contribution of the scalar diquark, which has the largest correlation length [13]: $\lambda_{0^+} := 1/m_{0^+} = 0.27$ fm. For all (ud) correlations with $J^P \neq 1^+$, $\lambda_{ud} < 0.5 \lambda_{0^+}$. The axial-vector correlation is different: $\lambda_{1^+} = 0.78 \lambda_{0^+}$, and it is quantitatively important in the calculation of baryon masses ($\approx 30\%$) [14]. Hence we anticipate that neglecting the 1^+ correlation will prove the primary defect of our ansatz. However, it is a helpful expedient in this exploratory calculation, which is made complicated by our desire to elucidate the effect of the diquarks' internal structure.

Our impulse approximation to the nucleon form factor is depicted in Fig. 1. Enumerating from top to bottom, the diagrams represent

$$\begin{aligned} \Lambda_{\mu}^1(q, P) = 3 \int \frac{d^4 l}{(2\pi)^4} \psi(K, p_3 + q) \Delta(K) \\ \times \psi(K, p_3) Q_F \Lambda_{\mu}^q(p_3 + q, p_3), \end{aligned} \quad (10)$$

with² $K = \eta P + l$, $p_3 = (1 - \eta)P - l$, $p_2 = K/2 - k$, $Q_F = \text{diag}(2/3, -1/3)$, $\Lambda_{\mu}^q(k_1, k_2) = S(k_1) \Gamma_{\mu}(k_1, k_2) S(k_2)$,

$$\begin{aligned} \Lambda_{\mu}^2(q, P) = 6 \int \frac{d^4 k}{(2\pi)^4} \frac{d^4 l}{(2\pi)^4} \Omega(p_1 + q, p_2, p_3) \\ \times \Omega(p_1, p_2, p_3) \text{tr}_D[\Lambda_{\mu}^q(p_1 + q, p_1) S(p_2)] \\ \times S(p_3) \frac{1}{3} I_F, \end{aligned} \quad (11)$$

which contributes equally to the proton and neutron and contains the diquark electromagnetic form factor, with $6 = \varepsilon_{c_1 c_2 c_3} \varepsilon_{c_1 c_2 c_3}$ and

² η describes the partitioning of the nucleon's total momentum, $P = p_1 + p_2 + p_3$, between the diquark and quark, a necessary feature of a covariant treatment.

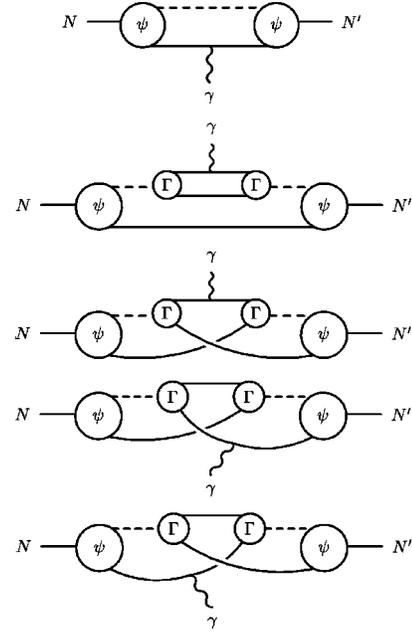


FIG. 1. Our impulse approximation to the electromagnetic current requires the calculation of five contributions, Eqs. (10)–(15). ψ : $\psi(l_1, l_2)$ in Eq. (8); Γ : Bethe-Salpeter-like diquark amplitude in Eq. (9); solid line: $S(q)$, quark propagator in Eq. (17); dotted line: $\Delta(K)$, diquark propagator in Eq. (28). The lowest three diagrams, which describe the interchange between the dormant quark and the diquark participants, effect the antisymmetrization of the nucleon's Faddeev amplitude. Current conservation follows because the photon-quark vertex is dressed, given in Eq. (23).

$$\Omega(p_1, p_2, p_3) = \psi(p_1 + p_2, p_3) \Delta(p_1 + p_2) \Gamma(p_1, p_2), \quad (12)$$

$$\begin{aligned} \Lambda_{\mu}^3(q, P) = 6 \int \frac{d^4 k}{(2\pi)^4} \frac{d^4 l}{(2\pi)^4} \Omega(p_1 + q, p_3, p_2) \\ \times \Omega(p_1, p_2, p_3) S(p_2) (i \tau_2)^T Q_F (i \tau_2) \\ \times \Lambda_{\mu}^q(p_1, p_1 + q) S(p_3), \end{aligned} \quad (13)$$

$$\begin{aligned} \Lambda_{\mu}^4(q, P) = 6 \int \frac{d^4 k}{(2\pi)^4} \frac{d^4 l}{(2\pi)^4} \Omega(p_1, p_3, p_2 + q) \\ \times \Omega(p_1, p_2, p_3) Q_F \Lambda_{\mu}^q(p_2 + q, p_2) S(p_1) S(p_3), \end{aligned} \quad (14)$$

$$\begin{aligned} \Lambda_{\mu}^5(q, P) = 6 \int \frac{d^4 k}{(2\pi)^4} \frac{d^4 l}{(2\pi)^4} \Omega(p_1, p_3 + q, p_2) \\ \times \Omega(p_1, p_2, p_3) S(p_2) S(p_1) Q_F \Lambda_{\mu}^q(p_3 + q, p_3). \end{aligned} \quad (15)$$

The nucleon-photon vertex is

$$\Lambda_{\mu}^q(q, P) = \Lambda_{\mu}^1(q, P) + 2 \sum_{i=2}^5 \Lambda_{\mu}^i(q, P). \quad (16)$$

Equation (16) is fully defined once $\Psi \sim \psi \Gamma \Delta$, S , and Γ_{μ} are specified. S and Γ_{μ} are primary elements in studies of meson properties and are already well constrained. For the dressed-quark propagator,

$$S(p) = -i\gamma \cdot p \sigma_V(p^2) + \sigma_S(p^2) \quad (17)$$

$$= [i\gamma \cdot p A(p^2) + B(p^2)]^{-1}, \quad (18)$$

we use the algebraic parametrizations [3]:

$$\bar{\sigma}_S(x) = 2\bar{m}\mathcal{F}(2(x+\bar{m}^2)) + \mathcal{F}(b_1x)\mathcal{F}(b_3x)[b_0 + b_2\mathcal{F}(\epsilon x)], \quad (19)$$

$$\bar{\sigma}_V(x) = \frac{1}{x+\bar{m}^2} [1 - \mathcal{F}(2(x+\bar{m}^2))], \quad (20)$$

with $\mathcal{F}(y) = (1 - e^{-y})/y$, $x = p^2/\lambda^2$, $\bar{m} = m/\lambda$, $\bar{\sigma}_S(x) = \lambda \sigma_S(p^2)$, and $\bar{\sigma}_V(x) = \lambda^2 \sigma_V(p^2)$. The mass scale, $\lambda = 0.566$ GeV, and parameter values

| \bar{m} | b_0 | b_1 | b_2 | b_3 |
|-----------|-------|-------|-------|-------|
| 0.00897 | 0.131 | 2.90 | 0.603 | 0.185 |

were fixed in a least-squares fit to light-meson observables. [$\epsilon = 10^{-4}$ in Eq. (19) acts only to decouple the large- and intermediate- p^2 domains.] This algebraic parametrization combines the effects of confinement and DCSB with free-particle behavior at large spacelike p^2 [2].

In Eqs. (10)–(15), Γ_μ is the dressed-quark-photon vertex. It satisfies the vector Ward-Takahashi identity,

$$(l_1 - l_2)_\mu i\Gamma_\mu(l_1, l_2) = S^{-1}(l_1) - S^{-1}(l_2), \quad (22)$$

which ensures current conservation [3]. Γ_μ has been much studied [16] and, although its exact form remains unknown, its qualitative features have been elucidated so that a phenomenologically efficacious ansatz has emerged [17]:

$$i\Gamma_\mu(l_1, l_2) = i\Sigma_A(l_1^2, l_2^2) \gamma_\mu + (l_1 + l_2)_\mu \left[\frac{1}{2} i\gamma \cdot (l_1 + l_2) \times \Delta_A(l_1^2, l_2^2) + \Delta_B(l_1^2, l_2^2) \right], \quad (23)$$

$$\Sigma_F(l_1^2, l_2^2) = \frac{1}{2} [F(l_1^2) + F(l_2^2)], \quad (24)$$

$$\Delta_F(l_1^2, l_2^2) = \frac{F(l_1^2) - F(l_2^2)}{l_1^2 - l_2^2}, \quad (25)$$

where $F = A, B$; i.e., the scalar functions in Eq. (18). A feature of Eq. (23) is that Γ_μ is completely determined by the dressed-quark propagator. Further, we estimate that calculable improvements would modify our results by $\lesssim 15\%$ [18].

The new element herein is the model of the nucleon's Faddeev amplitude, Eq. (8). For the Bethe-Salpeter-like amplitudes we use the one-parameter model forms

$$\Gamma(q_1, q_2) = \frac{1}{\mathcal{N}_\Gamma} \mathcal{F}(q^2/\omega_\Gamma^2), \quad q := \frac{1}{2}(q_1 - q_2) \quad (26)$$

TABLE I. A variation of the model parameters ω_ψ , ω_Γ , and m_Δ (in GeV) illustrates the sensitivity and stability of our results. The column labeled “ r_n ” lists $\text{sign}(r_n^2)|r_n^2|^{1/2}$. (Radii in fm, magnetic moments in units of μ_N . The statistical errors are $\lesssim 1\%$.)

| ω_ψ | ω_Γ | m_Δ | r_p | r_n | μ_p | μ_n | μ_n/μ_p |
|---------------|-----------------|------------|-------|-------|---------|---------|---------------|
| 0.20 | 1.0 | 0.63 | 0.79 | -0.43 | 2.88 | -1.58 | -0.55 |
| 0.16 | 1.0 | 0.63 | 0.84 | -0.46 | 2.83 | -1.55 | -0.55 |
| 0.24 | 1.0 | 0.62 | 0.75 | -0.41 | 2.89 | -1.59 | -0.55 |
| 0.20 | 0.8 | 0.62 | 0.80 | -0.40 | 2.93 | -1.64 | -0.56 |
| 0.20 | 1.2 | 0.63 | 0.78 | -0.45 | 2.84 | -1.54 | -0.54 |

$$\psi(l_1, l_2) = \frac{1}{\mathcal{N}_\Psi} \mathcal{F}(l^2/\omega_\Psi^2), \quad l := (1 - \eta)l_1 - \eta l_2. \quad (27)$$

Our impulse approximation is founded on a dressed-ladder kernel in the Faddeev equation and Γ_μ satisfies Eq. (22). Hence, the canonical normalization conditions for the diquark and nucleon amplitudes translate to the constraints that the (ud) diquark must have charge $1/3$ and the proton unit charge, which fix \mathcal{N}_Γ and \mathcal{N}_Ψ . For the diquark propagator we use the one-parameter form

$$\Delta(K^2) = \frac{1}{m_\Delta^2} \mathcal{F}(K^2/\omega_\Delta^2), \quad (28)$$

and interpret $1/m_\Delta$ as the diquark correlation length.

We fix the model's three parameters by optimizing a fit to $G_E^p(q^2)$ and ensuring $G_E^n(0) = 0$, which yields³

| | ω_ψ | ω_Γ | m_Δ |
|--------------|---------------|-----------------|------------|
| $\eta = 2/3$ | 0.20 | 1.0 | 0.63 |

all in GeV ($1/m_\Delta = 0.31$ fm). Using Monte-Carlo methods to evaluate the multidimensional integrals, these values give

| | Emp. | Calc. |
|----------------------|----------------------|----------------------|
| $r_p^2(\text{fm})^2$ | (0.87) ² | (0.79) ² |
| $r_n^2(\text{fm})^2$ | -(0.34) ² | -(0.43) ² |
| $\mu_p(\mu_N)$ | 2.79 | 2.88 |
| $\mu_n(\mu_N)$ | -1.91 | -1.58 |
| μ_n/μ_p | -0.68 | -0.55 |

where the statistical error is $\lesssim 1\%$. The sensitivity of our results to the model's parameters is illustrated in Table I. It is clear that the fit is stable but does not bracket the experimen-

³Our results are sensitive to η because Eqs. (26) and (27) are equivalent to retaining only the leading Dirac amplitude in the expression for these functions and neglecting their $q \cdot K$, $l \cdot P$ dependence when solving the Bethe-Salpeter and Faddeev equations. $\eta = 2/3$ is required for this ansatz to transform correctly under charge conjugation. Accounting for the $q \cdot K$, $l \cdot P$ dependence would eliminate this artifact [14,19].

TABLE II. Relative contribution to the charge radii and magnetic moments of each of the five diagrams in our impulse approximation: Fig. 1, Eqs. (10)–(15).

| Diagram | 1 | 2 | 3 | 4 | 5 |
|-------------------|------|-------|-------|------|------|
| $(r_p^2)^i/r_p^2$ | 0.68 | 0.11 | -0.02 | 0.12 | 0.12 |
| $(r_n^2)^i/r_n^2$ | 1.14 | -0.37 | -0.15 | 0.19 | 0.19 |
| μ_p^i/μ_p | 0.60 | 0.01 | 0.04 | 0.17 | 0.17 |
| μ_n^i/μ_n | 0.55 | -0.02 | 0.15 | 0.16 | 0.16 |

tal domain; i.e., the model lacks a relevant degree of freedom, a defect we expect the inclusion of an axial-vector diquark to ameliorate.

The charge radii are obtained via

$$r_{p,n}^2 = -6 \frac{d}{dq^2} F_1^{p,n}(q^2) \Big|_{q^2=0} + \frac{3}{2M^2} F_2^{p,n}(0), \quad (31)$$

$$:= (r_{p,n}^I)^2 + (r_{p,n}^F)^2 \quad (32)$$

and in this calculation (in fm²)

$$\begin{aligned} (r_p^I)^2 &= (0.70)^2, & (r_p^F)^2 &= (0.35)^2, \\ (r_n^I)^2 &= -(0.29)^2, & (r_n^F)^2 &= -(0.32)^2. \end{aligned} \quad (33)$$

A 20% reduction in ω_Γ (Table I, row 4) reduces $|r_n|$ by 7%. However, that results from a 21% reduction in $|r_n^I|$ and 2% increase in $|r_n^F|$. We attribute our overestimate of $|r_n^2|$ to a poor description of $F_1^n(q^2)$, which involves many cancellations between terms because of the (u,d,d) electric charge combinations and must vanish at $q^2=0$.

Five diagrams contribute to our impulse approximation and diagram 2 involves the diquark form factor. The calculated value of the associated elastic charge radius provides a measure of the size of the ‘‘constituent’’ diquark:

$$r_{0+}^2 = (0.45 \text{ fm})^2 = (0.80 r_\pi)^2, \quad (34)$$

with r_π calculated in the same model [3], and in quantitative agreement with another estimate [22]. This is important because, with ω_Γ allowed to vary, r_{0+} is a qualitative prediction of the model. Thus an optimal description of the data *requires* a nonpointlike diquark.

Table II provides a guide to each diagram’s relative importance. In all cases the first diagram, describing scattering from the dormant quark, is the most significant. For the charge radii the breakup contributions are comparable in magnitude to the second diagram, photon-diquark scattering. The magnetic moments are of particular interest. A scalar diquark does not have a magnetic moment, and that is expressed in our calculation by the very small contribution from diagram 2. It is not identically zero because of the *confinement* of the spectator quark; i.e., the absence of a mass shell. Diagrams 3–5 only appear because the diquark is a nonpointlike composite and they provide $\sim 50\%$ of μ_p, μ_n . Discarding these contributions one obtains $\mu_n/\mu_p \geq -0.5$, and in pointlike diquark models the axial-vector has

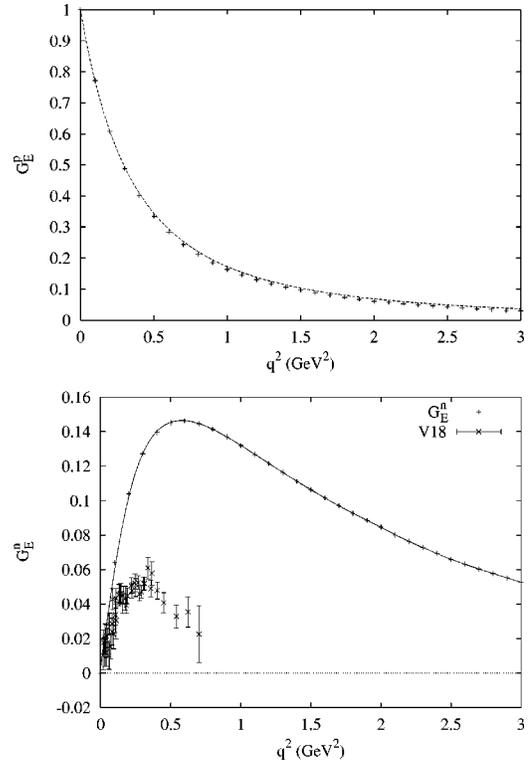


FIG. 2. Upper panel: Calculated proton electric form factor: +, compared with the empirical dipole fit: $F_{\text{emp}}(q^2) = 1/(1 + q^2/m_{\text{emp}}^2)^2$, $m_{\text{emp}} = 0.84$ GeV. Lower panel: Calculated neutron electric form factor: +, compared with the experimental data [20] as extracted using the Argonne V18 potential [21]. In both calculations the Monte-Carlo errors are smaller than the symbols.

alone been forced to remedy that defect [23]. Our results indicate that approach to be erroneous, attributing too much importance to the axial-vector correlation.

The calculated form factors are depicted in Figs. 2 and 3 and it is obvious in Fig. 2 that we used $G_E^p(q^2)$ to constrain our fit. The 0^+ (ud) diquark correlation in Ψ ensures that $G_E^{\text{fit}}(q^2) \neq 0$, and the presence of diquark correlations can also explain the N - Δ mass difference. Our result for $G_E^n(q^2)$ is well described by [20]

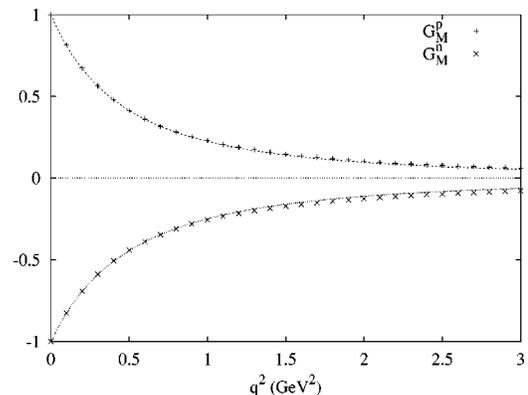


FIG. 3. Calculated proton and neutron magnetic form factors, normalized by $|\mu_{p,n}|$ in Eq. (30). The curves are dipole fits with masses (in GeV): $m_p = 0.95$, $m_n = 1.0$, 13% and 19% larger than m_{emp} in Fig. 2. [$\mu_{p,n}^{\text{emp}} F_{\text{emp}}(q^2)$ describes the data very well.]

$$G_E^n(q^2) = -\mu_n^{\text{emp}} F_{\text{emp}}(q^2) \frac{a^2 \tau}{1 + b^2 \tau}, \quad (35)$$

with $\tau = q^2/(2M)^2$, $F_{\text{emp}}(q^2)$ given in Fig. 2, and $a = 1.33$, $b = 1.00$, and the discrepancy between our calculation and experiment can be discussed in terms of these parameters. a characterizes the charge radius and it is $\lesssim 30\%$ too large, as can be anticipated from Eq. (30). b describes the magnitude at intermediate momenta and it is only $\sim 23\text{--}35\%$ of the empirical value. That is a systematic defect shared by other studies [24] that only retain the scalar diquark correlation. Unlike those studies, however, our calculated magnetic form factors, Fig 3, agree well with the data and, as we have seen, that is because we include the diquark breakup diagrams. It must be borne in mind that in our calculation a and b are *not* independent. Modifying the parameters in Eq. (29) so as to reduce a automatically and substantially increases b . However, notwithstanding our observation that its importance has previously been overestimated, without an axial-vector diquark correlation it is not possible to accurately describe all observables simultaneously.

We have employed a three-parameter model of the nucleon's Faddeev amplitude, Ψ , to calculate an impulse approximation to the electromagnetic form factors. Ψ represents the nucleon as a bound state of a confined quark and confined, nonpointlike scalar diquark, and the exchange of roles between the dormant and diquark-participant quarks is an integral feature. Five processes contribute: direct quark-photon scattering with a spectator diquark; photon-diquark scatter-

ing with a spectator quark; and three distinct diquark breakup diagrams. We obtain a good description of all form factors except G_E^n , which is too large in magnitude. That defect is shared by all models that do not include more than a scalar diquark correlation. The nonpointlike nature of the diquark correlation is important, especially via the breakup contributions which provide large contributions to the magnetic moments and ensure $\mu_n/\mu_p < -0.5$.

Including a nonpointlike axial-vector diquark is an obvious improvement of the model. That must be done in analogy with the scalar diquark because an accurate interpretation of the model parameters is impossible if the breakup diagrams are discarded. Another avenue for improvement is a direct solution of the Faddeev equation, retaining the axial-vector correlation and the breakup contributions to the form factor. That would provide a model for correlating meson and baryon observables in terms of very few parameters.

Models of the nucleon such as ours have hitherto been applied only at small and intermediate q^2 . Based on the observation [4] that a description of the large- q^2 behavior of $F_\pi(q^2)$ is only possible if the subleading pseudovector components of the pion's Bethe-Salpeter amplitude are retained, we anticipate that a successful description of the nucleon form factors on that domain will require a parametrization of the Faddeev amplitude that includes the analogous subleading Dirac components.

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- [1] C.D. Roberts and A.G. Williams, *Prog. Part. Nucl. Phys.* **33**, 477 (1994).
- [2] C.D. Roberts, *Fiz. Elem. Chastits At. Yadra* **30**, 537 (1999) [*Phys. Part. Nuclei* **30**, 223 (1999)].
- [3] C.J. Burden, C.D. Roberts, and M.J. Thomson, *Phys. Lett. B* **371**, 163 (1996).
- [4] P. Maris and C.D. Roberts, *Phys. Rev. C* **58**, 3659 (1998).
- [5] F.T. Hawes and M.A. Pichowsky, *Phys. Rev. C* **59**, 1743 (1999).
- [6] C.D. Roberts, *Fiz. B* **8**, 285 (1999).
- [7] P.C. Tandy, *Fiz. B* **8**, 295 (1999).
- [8] D. Klabučar and D. Kekez, *Fiz. B* **8**, 303 (1999).
- [9] R. Alkofer and C.D. Roberts, *Phys. Lett. B* **369**, 101 (1996).
- [10] R.T. Cahill, C.D. Roberts, and J. Praschifka, *Aust. J. Phys.* **42**, 129 (1989).
- [11] A. Bender, C.D. Roberts, and L. Von Smekal, *Phys. Lett. B* **380**, 7 (1996).
- [12] C.J. Burden, R.T. Cahill, and J. Praschifka, *Aust. J. Phys.* **42**, 147 (1989).
- [13] C.J. Burden, L. Qian, C.D. Roberts, P.C. Tandy, and M.J. Thomson, *Phys. Rev. C* **55**, 2649 (1997).
- [14] M. Oettel, G. Hellstern, R. Alkofer, and H. Reinhardt, *Phys. Rev. C* **58**, 2459 (1998).
- [15] A. Bender, "Probing Confined-Quark Dynamics via Nucleon Form Factors," in *Proceedings of the 14th International Conference on Particles and Nuclei*, edited by C.E. Carlson and J.J. Domingo (World Scientific, Singapore, 1997), pp. 669 and 670.
- [16] A. Bashir, A. Kizilersu, and M.R. Pennington, *Phys. Rev. D* **57**, 1242 (1998).
- [17] J.S. Ball and T. Chiu, *Phys. Rev. D* **22**, 2542 (1980).
- [18] R. Alkofer, A. Bender, and C.D. Roberts, *Int. J. Mod. Phys. A* **10**, 3319 (1995).
- [19] P. Maris and C.D. Roberts, *Phys. Rev. C* **56**, 3369 (1997).
- [20] S. Platchkov *et al.*, *Nucl. Phys.* **A510**, 740 (1990).
- [21] R.B. Wiringa, private communication; R.B. Wiringa, V.G. Stoks, and R. Schiavilla, *Phys. Rev. C* **51**, 38 (1995).
- [22] C. Weiss, A. Buck, R. Alkofer, and H. Reinhardt, *Phys. Lett. B* **312**, 6 (1993).
- [23] V. Keiner, *Phys. Rev. C* **54**, 3232 (1996).
- [24] G.V. Efimov, M.A. Ivanov, and V.E. Lyubovitsky, *Z. Phys. C* **47**, 583 (1990); V. Keiner, *Z. Phys. A* **354**, 87 (1996); G. Hellstern, R. Alkofer, M. Oettel, and H. Reinhardt, *Nucl. Phys.* **A627**, 679 (1997).