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Highly Birefringent Elliptical Core Photonic Crystal Fiber for Terahertz Application

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Abstract

We present a novel strategy for designing a highly birefringent photonic crystal fiber (PCF) with near zero flattened dispersion properties by applying elliptical air holes in the core area. The elliptical structure of the air holes in the porous-core region introduces asymmetry between $x$ and $y$ polarization modes, which consequently offers ultra-high birefringence. Also the compact geometry of the conventional hexagonal structure in the cladding confines most of the useful power. The optical properties including birefringence, dispersion, confinement loss, effective material loss (EML) and single modeness of the fiber are investigated using a full-vector finite element method. Simulation results show an ultra-high birefringence of 0.086 ultraflattened near zero dispersion of $0.53 \pm 0.07$ ps/THz/cm in a broad frequency range. The practical implementation of the proposed fiber is feasible using existing fabrication technology and is applicable to the areas of terahertz sensing and polarization maintaining systems.

Keywords: photonic crystal fiber, birefringence, dispersion, waveguide, effective material loss, terahertz.

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1. Introduction

The electromagnetic frequency band lying between the technologically well-developed microwave and infrared regions is generally referred to as the terahertz band. Recently, significant attention has been given to terahertz wave propagation due to its numerous practical applications in the field of sensing \[1\], non-invasive medical imaging \[2\], spectroscopy \[3\], detection of defects in solar panels, characterization of dielectric materials\[4\], pharmaceutical drug testing, astronomy, and communication \[5\]. Although there has been an enormous development in terahertz wave generation and detection, most of terahertz realizations are free-space systems. Free space propagation of terahertz waves is limited by moisture in the atmosphere. So, for low loss, flexible, long distance and efficient transmission of terahertz waves, it is necessary to design guided transmission media. Keeping all of this in mind, various types of guided transmission media have been proposed in the past few years. Metallic wires \[6\] and metal coated dielectric tubes\[7\] were proposed earlier but disregarded due to their higher bending loss and lower coupling efficiency. In recent times, there has been interest in polymer fibers such as polymer Bragg fiber, polystyrene foam, plastic fiber, hollow core fiber, solid core fiber and porous core photonic crystal fiber (PCF) \[8\],\[9\],\[10\]. Using porous core PCF has a number of important advantages such as lower material absorption loss, lower dispersion, geometries such as pitch size, air hole radius, and core radius can be readily selected. Beside low loss, it is also necessary to design a highly birefringent fiber that has key applications in terahertz sensing, communications, and terahertz heterodyne detection. There are basically two key methods for obtaining a highly birefringent terahertz fibers, one is to break the symmetry in the cladding region and another is to introduce asymmetry in the porous core. Several types of waveguide have been proposed earlier for low loss and highly birefringent terahertz waveguide. In 2009, Atakaraminas et al. \[11\] proposed a low loss, low dispersion, and highly birefringent PCF. They introduced an asymmetrical structure in the core resulting in a birefringence of 0.026. A squeezed lattice elliptical air hole based
terahertz fiber were proposed by Chen et al. [12] and resulted in a birefringence of the order of $10^{-2}$. A dual air hole unit core based PCF has been proposed by Hasanuzzaman et al. [13]. They were able to obtain a moderate birefringence of 0.033 with a material absorption loss of 0.43 dB/cm. However, they neglect to report the dispersion properties of their proposed fiber. A spiral photonic crystal fiber was proposed later [14] to obtain a birefringence of 0.0483 but with a higher EML of 0.085 cm$^{-1}$. The dispersion variation in this case was also high. Raonaqul et al. [15] proposed a dual asymmetrical PCF with a birefringence of 0.045. However, their obtained EML as well as dispersion variation was much higher. An oligo-porous core [16] and triple hole core [17] fibers have also been proposed that shows a birefringence of $3 \times 10^{-2}$ and $10^{-2}$ respectively. Recently, a birefringence value $1.19 \times 10^{-2}$ with high EML of 0.0689 cm$^{-1}$ has been exhibited by applying two layers of elliptical structure in the core [18].

In this letter, we introduce a novel Topas based photonic crystal fiber consisting of a conventional hexagonal structure in the cladding and a penta-hole elliptical structure in the core which simultaneously offering ultra-high birefringence and ultra-low near zero flattened dispersion. Several types of core structures including hexagonal [19], rhombic [20], dual hole unit [13], diamond [21], rectangular slot [22], oligo-porous [19], tri-air hole [17], hexagonal structure with elliptical shaped air holes [28] have previously been analyzed. However, to the best of our knowledge, penta-hole elliptical structure inside a hexagonal cladding has not been considered. Using the existing fabrication techniques, the proposed terahertz waveguide is feasible.

2. Design Methodology

The cross section of the proposed terahertz PCF is shown in Fig. 1. Five rings of hexagonal structure with larger air filling fraction of 0.90 are used to obtain flat dispersion properties also the penta-hole elliptical air holes in the core are use to increase birefringence. Full vector finite element based commercially
available software package Comsol v4.3b is used to design the proposed structure. A perfectly matched layer (PML) boundary condition with 9% radius of the fiber is used at the outer part of the PCF to reduce the effect of surrounding environment. In the cladding region, the diameter of each air is set to $d$. The distance of air holes lies in the same ring is denoted by $\Lambda_1$ and that lies in the other rings is denoted by $\Lambda$. They are related to one another by $\Lambda_1 = 0.9\Lambda$. The core diameter is fixed to 350 $\mu$m. The diameter of the major and minor axis of the elliptical air holes has been denoted by $(L)$ and $(w)$ as shown in Fig. 1. For our simulation, we kept the major axis $(L)$ fixed and varied the minor axis $(w)$ by varying the core porosity. Furthermore, ellipticity defined as the ratio of major and minor axis of the elliptical air holes $(L/w)$ determines the size of the elliptical air holes. Different lengths have been used to design the elliptical air holes inside the core. The center air hole has a length $(L)$ of 255 $\mu$m; from the center air hole the length of other air holes both in upper and lower has a length of 160 $\mu$m and 130 $\mu$m respectively. The width $(w)$ of each air hole in the core has been determined by the core porosity that can be defined as the fiber core area to the total area of the fiber. Also the core pitch $P_c$ which can be defined as the center to center distance between two elliptical air holes has set to 6 $\mu$m. Topas has been used as the background material.

Figure 1: Schematic diagram of the proposed waveguide with its enlarged version of the core.
because of its unique characteristics including, lower bulk material absorption loss 0.2 cm\(^{-1}\); glass transition temperature \(T_g\) much higher than PMMA; multiantibody bio-sensing; constant refractive index \(n = 1.53\) in the frequency range of 0.1–1.5 THz; and being negligibly hygroscopic \[4, 23\]. Throughout the whole simulation 50\% porosity, 1 THz frequency and \(x\)-polarization mode is considered as optimum design parameters.

3. Simulation and Results

The mode power distribution at different core porosities for both \(x\) and \(y\) polarization is shown in Fig. 2. It is observed that, there is a large difference between the mode field distributions through the core region. As a result, there is a large effective index difference with respect to frequency between the polarization modes (Fig. 3). This is because of the large asymmetrical structure of the core air holes. The refractive index difference in the \(x\) and \(y\) polarization mode is known as birefringence. Birefringence can be calculated using the following equation \[28\],

\[
B = |n_x - n_y|
\]

where \(n_x\) and \(n_y\) represents the effective refractive index of \(x\) and \(y\) polarizations respectively. At different porosity values, Fig. 4 exhibit the characteristic sof birefringence variation with respect to frequency. It can be observed that, birefringence increases with the increase of frequency because such increments enhances the index contrast between the orthogonal polarization modes.
It is also observed that, at higher porosity values the amount of birefringence decreases because such increment of porosity causes some of the useful power propagates outside the core region that reduces the index contrast between the polarization modes which consequently reduces the birefringence. At optimal design parameters, the obtained birefringence is 0.086, which is better than the previously proposed [11, 12, 13, 14, 15, 16, 17, 18, 28] terahertz waveguides.

Figure 3: Effective refractive index vs frequency at optimal design parameters.

Figure 4: Birefringence vs frequency at different porosities with 350 µm core diameter.
The main difficulty of designing a terahertz waveguide is its high EML. So, for efficient transmission of terahertz waves it is necessary to design a low loss waveguide. The material absorption loss or EML of a fiber can be calculated by [27],

\[ \alpha_{\text{eff}} = \sqrt{\frac{\varepsilon_0}{\mu_0}} \left( \frac{\int_{\text{mat}} n_{\text{mat}} |E|^2 \alpha_{\text{mat}} dA}{\int_{\text{all}} S_z \, dA} \right). \]  

(2)

Here, \( n_{\text{mat}} \) is the effective refractive index of Topas COC, \( \alpha_{\text{mat}} \) is the bulk material absorption loss of Topas, \( \varepsilon_0 \) and \( \mu_0 \) is the relative permittivity and permeability of free space, \( S_z \) is the \( z \)-component of the Poynting vector \( S_z = \frac{1}{2}(E \times H^*)_z \). where \( E \) and \( H^* \) are the electric and magnetic field components. The effective material loss as a function of frequency is shown in Fig. 5. It can be observed that, as the frequency increases the EML also increases linearly which meets the theoretical consequences of calculating EML according to the empirical formula \( \alpha(\nu) = \nu^2 + 0.63\nu - 0.13 \) [dB/cm], [27]. It is also observed that, EML increases with the decrease of porosity because reducing porosity means reducing the core air hole diameter which in turn increase the amount of material inside the core area. At optimal design parameters, a very small amount of EML of 0.05 cm\(^{-1}\) is obtained which is comparable with the previously reported [11, 12, 13, 14, 15, 16, 17, 18] fibers.

![Figure 5: EML vs frequency at different porosities and 350 \( \mu \)m core diameter.](image)
Confinement loss is another loss mechanism which limits the length of terahertz signal transmission. This confinement loss occurs due to the finite number of air hole rings in the cladding that can be calculated by the following equation [26],

\[ L_c = 8.686 \left( \frac{2\pi f}{c} \right) \text{Im}(n_{\text{eff}}), \text{dB/cm}. \]  

(3)

Here, \( \text{Im}(n_{\text{eff}}) \) represents the imaginary part of the complex refractive index, \( f \) is the operating frequency and \( c \) is the speed of light. It is seen in Fig. 6 that, confinement loss rapidly drops with increase in frequency because the mode power begins to constrict strictly in the porous core region [27]. It is found that, a very low confinement loss of the order of \( 10^{-9} \text{ cm}^{-1} \) is obtained at optimal design parameters. It can be mentioned that; the obtained value of confinement loss is negligible compared to the obtained EML.

![Figure 6: Confinement loss vs frequency at optimal design parameters.](image)

Low and flat dispersion is impressive for applications in the terahertz frequency range. Dispersion properties of a fiber can be calculated by [28],

\[ \beta_2 = \frac{2}{c} \frac{dn_{\text{eff}}}{dw} + \frac{w}{c} \frac{d^2n_{\text{eff}}}{dw^2}, \text{ps/THz/cm}. \]  

(4)
Where, $c$ is the speed of light, $n_{\text{eff}}$ is the effective refractive index of the core, $\omega$ is the angular frequency. Fig. 7 indicates the dispersion variation with respect to frequency. It can be seen that, at optimal design parameters the obtained dispersion is $0.53 \pm 0.07$ ps/THz/cm within a broad frequency range of 0.5–1.48 THz. The obtained dispersion is very low and flat also significantly improved over previously reported optical waveguide designs [11, 12, 13, 14, 15, 16, 17, 18, 24, 25, 26, 27, 28].

Long-distance transmission of signals with nearly zero interference requires the use of single-mode PCF. The single mode condition of a fiber can be calculated using equation [29],

$$V = \frac{2\pi f}{c} \sqrt{n_{\text{co}}^2 - n_{\text{cl}}^2} \leq 2.405.$$  \hspace{1cm} (5)

Here, $n_{\text{co}}$ and $n_{\text{cl}}$ represents the effective refractive index of the core and cladding respectively. From the waveguide design, it can be observed that, the cladding mainly consists of a large number of air holes, thus most of the previously reported [24, 14] waveguides considered that value as unity, but practically the value should be greater than unity [27] because the cladding not only consists of air holes but also consists of bulk material. The value of $n_{\text{co}}$ is equal to the effective refractive index of the core. In Eqn. 5 it is clearly stated that, to operate a fiber into single mode region the value of $V$-parameter must not exceed 2.405.
So, observing Fig. 8 it can be said that, our proposed waveguide operates in the single mode condition.

Figure 8: V-parameter vs frequency at optimal design parameters.

For practical implementation of our proposed waveguide, it is necessary to address the fabrication possibilities thoroughly. There are several fabrication techniques developed in recent years. Among them, capillary stacking, stack and drilling, sol-gel techniques are only capable of fabricating circular shaped air holes. To fabricate asymmetrical structures Atakaramians et al. [11], [28] experimentally employed an extrusion technique [29]. Issa et. al [33] fabricated elliptical air holes in 2004. Moreover, the previously published articles [34] [35] [36] reported that the elliptical air hole patterns can be fabricated using the existing fabrication technology. In addition, Liu et al. [37] used the methyl methacrylate (MMA) monomer polymerization method to fabricate elliptical air holes. Moreover, Jiang et al. [30] recently used 3D printed dies and got improvement of fiber drawing over “stack and draw” and extruded preforms. They used the 3D printed technique to fabricate not only elliptical air holes but also other complex structures. Moreover, Microstructured optical fibers (MOFs) with different sizes of core and cladding air holes has already been fabricated using the extrusion technique [38], [39]. As our proposed waveguide consists of conventional hexagonal structure in the cladding and elliptical structure in the core, it is amenable to existing fabrication techniques.
In Table 1 the characteristics comparison of our proposed PCF with some other terahertz waveguide. It is clearly seen that, the proposed PCF shows excellent characteristics for polarization maintaining terahertz application in addition for flattened dispersion application. Using the elliptical air hole structure in the core, the obtained birefringence is highest than ever proposed by any terahertz waveguide.

Table 1: Comparison of characteristics of the proposed PCF with other PCF’s

<table>
<thead>
<tr>
<th>Ref.</th>
<th>$f$ (THz)</th>
<th>Por(%)</th>
<th>$B$</th>
<th>$\beta_2$(ps/THz/cm)</th>
<th>$\alpha_{eff}$</th>
<th>$L_c$</th>
</tr>
</thead>
<tbody>
<tr>
<td>[13]</td>
<td>0.85</td>
<td>-</td>
<td>0.033</td>
<td>-</td>
<td>0.43 dB/cm</td>
<td>$10^{−3.8}$ cm$^{-1}$</td>
</tr>
<tr>
<td>[14]</td>
<td>1</td>
<td>-</td>
<td>0.0483</td>
<td>0.51</td>
<td>0.085 cm$^{-1}$</td>
<td>0.00191 dB/cm</td>
</tr>
<tr>
<td>[15]</td>
<td>1</td>
<td>-</td>
<td>0.045</td>
<td>0.26</td>
<td>0.08 cm$^{-1}$</td>
<td>-</td>
</tr>
<tr>
<td>[16]</td>
<td>3</td>
<td>30</td>
<td>0.03</td>
<td>0.2 – 1</td>
<td>0.06 cm$^{-1}$</td>
<td>0.01 dB/m</td>
</tr>
<tr>
<td>[17]</td>
<td>3</td>
<td>60</td>
<td>0.01</td>
<td>0 – 1.5</td>
<td>0.04 cm$^{-1}$</td>
<td>0.01 dB/m</td>
</tr>
<tr>
<td>[18]</td>
<td>1</td>
<td>55</td>
<td>0.0119</td>
<td>-</td>
<td>0.068 cm$^{-1}$</td>
<td>- dB/cm</td>
</tr>
<tr>
<td>[31]</td>
<td>1</td>
<td>84</td>
<td>-</td>
<td>0.09</td>
<td>0.034 cm$^{-1}$</td>
<td>$10^{−3.7}$ cm$^{-1}$</td>
</tr>
<tr>
<td>[32]</td>
<td>1</td>
<td>83</td>
<td>-</td>
<td>0.05</td>
<td>0.03 cm$^{-1}$</td>
<td>$10^{6.5}$ cm$^{-1}$</td>
</tr>
<tr>
<td>This</td>
<td>1</td>
<td>50</td>
<td>0.086</td>
<td>0.07</td>
<td>0.05 cm$^{-1}$</td>
<td>$10^{9}$ cm$^{-1}$</td>
</tr>
</tbody>
</table>
4. Conclusion

A novel photonic crystal fiber with ultra-high birefringence and near zero flattened dispersion has been proposed. Numerical results indicate a very high birefringence of 0.086 and near zero flat dispersion 0.53±0.07 ps/THz/cm can be obtained within a broad frequency range of 0.5–1.48 THz. In addition, the proposed waveguide exhibits a negligible confinement loss of 10^{-9} cm^{-1} at 1 THz frequency. Potential applications are anticipated in the areas of sensing, terahertz communication systems and polarization preserving fibers.

References


