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ABSTRACT

The development and improvements in wind energy conversion systems (WECSs) are intensively focused these days because of its environment friendly nature. One of the attractive development is the maximum power extraction (MPE) subject to variations in wind speed. This paper has addressed the MPE in the presence of wind speed and parametric variation. This objective is met by designing a generalized global sliding mode control (GGSMC) for the tracking of wind turbine speed. The nonlinear drift terms and input channels, which generally evolves under uncertainties, are estimated using feed forward neural networks (FFNNs). The designed GGSMC algorithm enforced sliding mode from initial time with suppressed chattering. Therefore, the overall maximum power point tracking (MPPT) control is very robust from the start of the process which is always demanded in every practical scenario. The closed loop stability analysis, of the proposed design is rigorously presented and the simulations are carried out to authenticate the robust MPE.

INDEX TERMS

Feed forward neural networks (FFNNs), generalized global sliding mode controller (GGSMC), maximum power point tracking (MPPT), permanent magnet synchronous generator (PMSG), wind energy conversion systems (WECSs).

I. INTRODUCTION

Due to industrialization and increasing usage of electrical devices, the energy demand is increasing every day. Fossil fuels, which are becoming scarce nowadays are the main cause of global warming. Therefore the world energy experts investigate an alternate efficient and environment friendly energy resources. Wind energy, which is one of the investigated resource, attracted great attention because of its safety and cleanliness [1]. At the end of 2017, 52 giga watt (GW) of wind energy was added to the global installed capacity, and made a total of 539 GW [2].

The WECSs, based on speed, are categorized as fixed speed and variable speed WECSs. In the fixed speed WECSs, the generator speed remains constant and they are connected to the grid without using power converters. In variable speed WECSs, the speed of the generator is continuously adopted and controlled in such a manner that the turbine always operates at its maximum efficiency. Consequently, the MPE phenomena occurs which increased the annual product by 5-10% [3]. Note that, the operating region of wind turbine is divided into four regions as depicted in Fig. 4. Region 1 covers operation from the startup to the cut-in speed. The sub operated region, called Region 2, is from cut-in to rated speed. In Region 3, the speed regulation region, the goal is speed regulation at rated levels because the wind speed remains high enough to drive the generator at its rated output power. Region 4 occurs after the cut-out speed in which the turbine is shut down to avoid any damage because of high wind speed [4]. It is worthy to note that maximum power can be extracted from the WECSs by operating the turbine in the starting and rated wind speed.

WECSs, equipped with variable speed permanent magnet synchronous generator (VS-PMSG), are becoming popular...
day by day because of its higher efficiency, low weight, less maintenance, easy to control and no need for reactive and magnetizing current [5], [6]. The PMSG are generally operated by using a drive train technology [7] which builds coupling between the wind turbine and PMSG. In WECSs different power electronic converter with different topologies have been used to connect the generator (i.e. PMSG) to the grid. These power interfaces, work as control unit for the MPE and build grids connection capability [8].

WECSs observe low cost installation with environment friendly nature, but suffer from low-efficiency due to varying wind speed. To increase the efficiency, they must be operated at the maximum power point (MPP). Thus MPP performs as an important part of a WECS. Sufficient work is done in the development of efficient MPPT controllers. Numerous MPPT control techniques are used for VS-PMSG which make it possible to continuously adapt the rotational speed of VS-PMSG relative to the wind speed. This resulted in enhanced efficiency of wind turbine with decreased power fluctuations [9], [10]. In MPPT one search for the maximum coefficient of performance ($C_p$) subjected to varying wind speed. Two broad categories i.e conventional design and soft computing design strategy, for the MPPT design, one focused extensively in the existing literature.

Among the conventional techniques, perturbation and observation (P&O) or hill climbing search (HCS) is the simplest (see for details [11]). The drawbacks of this method is that it does not work well for fast varying wind speed as well as for large inertia wind turbines [12]. The selection of optimum step size is also a difficult job in this method.

Thus researchers were fascinated by soft computing techniques which are classified as Bio-inspired methods and artificial intelligence (AI) methods. The Bio-inspired techniques includes particle swarm optimization (PSO) [13], ant colony optimization (ACO) [14] and genetic algorithms (GA) [15]. These MPPT controllers under varying wind speed, showed fast convergence as compared to conventional methods. However these methods need many parameters such as population size, mutation, selection of chromosomes and crossover rate. In addition, the estimation of these parameters is itself a complex job. Under varying wind speed, all these parameters need to be readjusted, otherwise one cannot track MPP correctly.

The AI strategies, for the MPPT of WECSs, include fuzzy logic (FL) based [16], [17] controllers and artificial neural networks (ANN) [18], [19]. These techniques work with variable inputs, without exact mathematical modelling along with self convergence and self learning capabilities. On addition they have adaptive nature for nonlinear behavior of the systems. The FL method [16], [17] harvested maximum power from the wind but the dependency of the tracking performance and output efficiency on the engineer’s technical knowledge and the rules base table reduces its applicability. It also needs a lot of theoretical knowledge and may not guarantee an optimal response. The ANN [18] was employed for pitch controller design for a grid connected wind turbine system to harvest maximum power from available wind. Its performance was superior to conventional controllers. The ANN based MPPT controllers have better performance and effectiveness than the conventional and bio-inspired techniques. However, this requires months for training because of large memory size. In addition, it needs periodic tuning with the passage of time.

Other control techniques like proportional integral (PI) [20], quantitative feedback theory (QFT) [21] and Linear-quadratic-Gaussian (LQG) control technique [22] are also used for the MPPT of WECSs. All these techniques required a lot of computational and graphical analysis and have oscillating output power due to its non-robust nature.

Sliding mode control (SMC), introduced in 1950s, is famous for its versatile nature because it can be employed to both linear and nonlinear systems. It is also famous for its robust nature which is always claimed in sliding mode with reduced order dynamics. The order reduction, in sliding mode, provides insensitivity to parametric variations and disturbance of matched kind. It also demonstrates finite time convergence with good dynamic behavior and simple implementation [23], [24]. In order to deal with the unmatched uncertainties effects, an SMC strategy was synthesized with an uncertainty observer in [25] which showed very good results. In the context of intelligent designs, an SMC along with fuzzy logic was presented for uncertain descriptor systems in [26]–[28]. It is important to report here that very impressive but summarized developments in SMC, technical research issues and future perspectives regarding the SMC, are presented in [29], [30]. Having witnessed very appealing developments, the theory of SMC and its applications are still focused areas among the researchers. In the context of applications to power systems, a direct power control (DPC) based on SMC was proposed for the grid connected WECS in [31]. When the grid voltages becomes unbalanced then the SMC controller regulate the instantaneous active and reactive powers directly in stator stationary reference frame. To improve the control efficiency and performance of SMC used in PMSG-based WECS an exponential reaching law, a necessary part of the sliding mode controller, was proposed in [32]. Since, the dynamics of the wind power system is very stochastic and uncertain, therefore, an adaptive second-order SMC was presented in [33]. This work dealt effectively the presence of model uncertainties and the intrinsic nonlinear behavior of WECS. A proportional integral type sliding surface based SMC was proposed for renewable energy conversion systems and the electric motor drives in [34], [35]. At this stage, in the context of SMC applications to power systems, we want to attract the focuss of the readers to an important point that conventional SMC experiences reaching phase which reduces the robustness property of the SMC and it also causes chattering across the sliding constraint. Different techniques have been used to eliminate the reaching phase and to reduce the chattering effects (see for instance [36]). Since the amplitude of chattering phenomena is generally proportional to the amplitude of unknown dynamics e.g drift terms, input channels and disturbances. Therefore, in this work,
the uncertain nonlinearities (i.e. drift terms and input channel) are accurately estimated via the FFNNs. Consequently, the chattering is suppressed because the uncertainty bound (for a sliding mode) will be a bit smaller in this adaptive case. In addition, the surface across which the sliding mode is enforced is an integral type which also results in chattering suppression along with enhanced robustness. The chattering suppression is also targeted via the use of a strong reachability law. The use of this reachability law gives us fast sliding mode enforcement time. The elimination of reaching phase, which often results in decreased robustness, is also a target in this work. Therefore, a FFNNs based robust GGSM MPPT control law is developed in this paper which is quite fascinating to investigate. The closed loop stability analysis and states convergence is ensured mathematically and simulations (in MATLAB environment) are carried out to authenticate the claim. The developed results are also compared with standard literature results [37].

The rest of the paper is structured as follow. The detail of WECS is given in Section 2 and input-output form of the considered system is presented in Section 3. The FFNN, used for the estimation of unknown terms and analysis of the proposed control technique, is discussed in Section 4 and section 5 respectively. Simulation results under varying wind speed is given in Section 6. In Section 7, the performance of the proposed controller is compared with standard feedback linearization approach. Finally, the conclusion is presented in Section 7.

II. MODELLING OF WECS
The model of WECS which will be studied in this paper is shown in Fig. 1. It mainly consists of a turbine, a gear box, converters and a variable speed wind turbine which is equipped with a PMSG and is further connected to a grid. The system illustrated in Fig. 2, is an equivalent model of the system of Fig. 1. The variable resistance $R_l$ and the constant inductance $L_s$ are the control variables in which $L_s$ is kept fixed and $R_l$ is adjusted to extract maximum power.

Now the detailed presentation of wind turbine model, drive train and PMSG will be given in the following study.
**A. WIND TURBINE MODEL**

The fundamental equation governing the mechanical power captured by the turbine from wind is given as [38]:

\[ P_{\text{mech}} = \frac{1}{2} \rho A V^3 C_p(\lambda, \beta) \]  

(1)

where \( \rho \) is the air density (kg/m\(^3\)), \( C_p \) is the power coefficient, \( A \) is the area of the blades (m\(^2\)), \( V \) is the average wind speed (m/s), \( \lambda \) is the tip speed ratio and \( \beta \) is the pitch angle. As the wind speed increases the mechanical output power of wind turbine significantly increases as clearly seen in Fig. 3.

**FIGURE 3. Wind turbine speed vs output mechanical power.**

The tip speed ratio is defined as

\[ \lambda = \frac{\omega_h R_t}{V} \]  

(2)

where \( R_t \) is the radius of the turbine(m) and \( \omega_h \) is the angular speed of the high speed shaft. Note that \( C_p \) is a non-linear function of lambda \( \lambda \) and beta \( \beta \), whose values varies from system to system. The detailed mathematical expression of \( C_p \) is given as [39]:

\[ C_p = (0.5 - 0.0167(\beta - 2) \text{sin} [(\frac{\pi (\lambda + 0.1)}{18 - 0.3(\beta - 2)}) - 0.00184(\lambda - 3)(\beta - 2)] \]  

(3)

The theoretical upper limit of \( C_p \), also known is Betz coefficient, is 0.47 [40]. For different values of beta, the \( C_p \) characteristic curve is shown in Fig. 4. By changing \( \lambda \) and \( \beta \), the \( C_p \) is changing. At a specific \( \lambda \) called lambda optimum (\( \lambda_{\text{opt}} \)) the value \( C_p \) is maximum which is called \( C_{p\text{max}} \). By following the \( C_{p\text{max}} \) curve, the variable speed wind turbine gets maximum power from the wind (i.e., by varying the rotor speed to keep the system at rated speed and \( \lambda_{\text{opt}} \)).

**B. DRIVE TRAIN MODEL**

By neglecting the stiffness and damping factor, the one-mass drive train model [37] is described as

\[ J \frac{d\omega_h}{dt} = T_a - T_{\text{em}} \]  

(4)

where \( J \) is the inertia constant of the high speed shaft, \( T_a \) is the aerodynamic torque and \( T_{\text{em}} \) is the electromagnetic torque.

**FIGURE 4. Wind turbine operation regions.**

Note that the mechanical power, in term of \( T_a \) and \( \omega_h \), looks as follows

\[ P_{\text{mech}} = T_a \omega_h \]  

(5)

The ratio between \( C_p \) and \( \lambda \) appear as follows

\[ C_q = \frac{C_p(\lambda, \beta)}{\lambda} \]  

(6)

Incorporating (1) and (2) in (5), one may get

\[ T_a = \frac{1}{2}(\rho \pi r^3)C_q V^2 \]  

(7)

For the purposes of optimal control, the \( C_q \) in term of \( \lambda \) is approximated as follows

\[ C_q(\lambda) = a_0 + a_1 \lambda + a_2 \lambda^2 \]  

(8)

Using (2) in (8) and then incorporating it in (7), the aerodynamic torque \( T_a \) becomes

\[ T_a = d_1 V^2 + d_2 \omega_h + d_3 \omega_h^2 \]  

(9)

where

\[ d_1 = \frac{1}{2} \pi \rho R_t^3 a_0, \quad d_2 = \frac{1}{2} \pi \rho R_t^4 a_1, \quad d_3 = \frac{1}{2} \pi \rho R_t^5 a_2 \]  

(10)

with

\[ a_0 = 0.1253, \quad a_1 = -0.0047, \quad a_2 = -0.0005 \]  

(11)

**C. PMSG MODEL**

Having performed Park’s transformation and eliminating \( v_o \), the PMSG model can be described by the following dynamics [37].

\[ v_d = R_i i_d + L_d \frac{di_d}{dt} - L_q i_q \omega_s \]  

(12)

\[ v_q = R_i i_q + L_q \frac{di_q}{dt} + (L_d i_d + \phi_m)\omega_s \]  

(13)

where \( R \) is the stator resistance, \( v_d, v_q \) are \( d \) and \( q \) stator voltages, \( L_d \) and \( L_q \) are the \( d \) and \( q \) inductances, \( \omega_s \) is the stator pulsation and \( \phi_m \) is the flux that is constant due to permanent magnets.
The electromagnetic torque is expressed as

$$T_{em} = p[\phi mi_q + (L_d - L_q)i_di_q]$$  \hspace{1cm} (14)$$

where $p$ is the number of pole pairs. If the permanent magnet is mounted on the rotor surface, then $L_d$ becomes equal to $L_q$. Consequently,

$$T_{em} = p\phi mi_q$$  \hspace{1cm} (15)$$

The non-linear equations for a PMSG, when connected to a grid, is described as [37]

$$\dot{i}_d = -\frac{1}{L_d + L_s} [(R + R_l)i_d + p(L_q + L_s)i_q\omega_h]$$

$$\dot{i}_q = -\frac{1}{L_q + L_s} [(R + R_l)i_q - p(L_d + L_s)i_d\omega_h + p\phi_m\omega_h]$$

$$\dot{\omega}_h = \frac{1}{J} (T_u - p\phi_m i_q)$$  \hspace{1cm} (16)$$

while $R_l$ is the load resistance and $L_q$ is the load inductance and $(\omega_h = \omega_x i$ and $i$ is the gear ratio).

The system (16), in general form, can be expressed as

$$\begin{align*}
\dot{x} &= f(x) + g(x)u \\
y &= h(x)
\end{align*}$$  \hspace{1cm} (17)$$

where $i_d$, $i_q$, and $\omega_h$ is considered as $x_1$, $x_2$, and $x_3$, respectively, and $R_l$ is replaced with $u$. In addition,

$$f(x) = \begin{bmatrix}
\frac{1}{L_d + L_s}(-Rx_1 + p(L_q - L_s)x_2x_3) \\
\frac{1}{L_q + L_s}(-Rx_2 - p(L_d + L_s)x_1x_3) + p\phi_m x_3 \\
\frac{1}{J}(d_1v^2 + d_2x_3 + d_3x_2^2 - p\phi_m x_2)
\end{bmatrix} \in \mathbb{R}^3 \\
- g(x) = \begin{bmatrix}
\frac{1}{L_d + L_s}x_1 \\
\frac{1}{L_q + L_s}x_2 \\
0
\end{bmatrix} \in \mathbb{R}^3, u$$

and $y = h(x) = x_3 = \omega_h$ is the output of the plant.

$$\begin{align*}
\text{(18)}
\end{align*}$$

III. INPUT-OUTPUT FORM

For our control strategy, the most suitable form is the input-output form of the (18) as in [37], [41] which is represented as by defining the following transformation.

$$\begin{align*}
z_1 &= y = h(x) = x_3 = \omega_h \\
z_2 &= L_f h(x) = \frac{\partial h(x)}{\partial x} f(x) = m_1 - m_2x_3 + m_3x_2 - m_4x_2 \\
z_3 &= L_f^2 h(x) = \frac{x_1}{x_2}
\end{align*}$$  \hspace{1cm} (19)$$

Since the relative degree, $r$ of the system is one, less than the system order $n$ i.e., $(r < n)$, so the input-output form appears as follows

$$\begin{align*}
\dot{z}_1 &= z_2 \\
\dot{z}_2 &= L_f^2 h(x) + L_f L_g h(x)u
\end{align*}$$  \hspace{1cm} (20)$$

$$\begin{align*}
\dot{z}_3 &= \frac{m_4}{m_1} (- \frac{k_1x_3}{m_1} - \frac{k_2x_1}{m_4} - \frac{k_3x_3u}{m_4} \\
&= (\frac{z_3}{m_1}) m_4^2 \left( - \frac{l_3x_1}{m_4} - \frac{l_2x_1x_3}{m_4} + l_3x_3 \right)
\end{align*}$$  \hspace{1cm} (21)$$

The parametric values of the under study model is given in table 1. The values of the derived parameters are calculated by using the typical parameters given in the table 2 and 3 (see for more details [37], [41]).

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_1$</td>
<td>27.39023</td>
<td>$k_2$</td>
<td>-0.98766</td>
</tr>
<tr>
<td>$k_3$</td>
<td>-8.22639</td>
<td>$l_1$</td>
<td>27.34708</td>
</tr>
<tr>
<td>$l_2$</td>
<td>-3</td>
<td>$l_3$</td>
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<td>$m_2$</td>
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<td>$m_3$</td>
<td>-0.00560</td>
</tr>
<tr>
<td>$m_4$</td>
<td>-23.8152</td>
<td>$d_1$</td>
<td>3.6442</td>
</tr>
<tr>
<td>$d_2$</td>
<td>-0.3605</td>
<td>$d_3$</td>
<td>-0.0959</td>
</tr>
</tbody>
</table>

So, one of the transformed state i.e., $z_3$ is of zero dynamics. Now, it is necessary to discuss the stability of the zero-dynamics.

A. ZERO-DYNAMICS STABILITY INVESTIGATION

The nonlinear system’s dynamics are divided into 2 parts i.e., an internal part and an external (input-output) part, when performing the input-output conversion. Since, the external dynamic states i.e., $(z_1$, $z_2$) are controllable states and are directly controlled by $u$ while the stability of the internal dynamic state i.e., $(z_3)$ is simply determined by the location of zeros called zero-dynamics for a nonlinear system [42]. To calculate the zero dynamics, the following variables should be set to zero i.e., $z_1 = z_2 = u = 0$ in (21). By simplifying (21), finally one gets

$$\dot{z}_3 = -z_3(k_1 - l_1)$$  \hspace{1cm} (22)$$

where $k_1 > l_1$, so

$$\dot{z}_3 = -Kz_3$$  \hspace{1cm} (23)$$

where $K$ is a positive integer. So the zero-dynamic state $z_3$ is stable as long as $k_1 > l_1$.

Remark 1: The third order nonlinear system (reported in (19)) with two visible states i.e., $z_1$, $z_2$ and one internal dynamics state, is considered for the controller design which will be discussed in details in the control design section.

IV. UNKNOWN TERMS ESTIMATION

This section presents the estimation of the nonlinear drift term $L_f^2 h(x)$ and input channel $L_g L_f h(x)$ for the input-output form developed in the previous section. The estimation is done via FFNNs which will be discussed below.
under study procedure is shown in Fig. 6.

The non-linear function estimation. The schematic diagram of $z$ where $j$ for this nonlinear approximation will include the states $z_1$, $z_2$, $z_3$ and $V$. A three layer FFNN is an efficient method for NNs learns to create a mapping between these independent variables and dependent output [44]. The training set in NNs consists of ten neurons with sigmoid function as an activation function. The third layer is an output layer which gives us the output layer computes its net activation as follow

$$a_k = \sum_{j=1}^{l_o} \omega_{kj}y_j + b_{ko},$$

(26)

where $k$ is the number of neuron in the output layer, $\omega_{kj}$ is scalar called weight between the $k^{th}$ output layer node and the $j^{th}$ hidden layer node. The output layer produces an outputs $L^2_J h(x)$ and $L_gL_f h(x)$ as a function of its net activation as follows

$$\begin{align*}
\{L^2_J h(x) &= f_1(a_k) \\
L_gL_f h(x) &= f_2(a_k)
\end{align*}$$

(27)

The output of the estimated model can be expressed as the function of the inputs, the weights between input and hidden layer and the weights between the hidden and the output layer which is described as follows

$$\begin{align*}
\{L^2_J h(x) &= f_1 \left( \sum_{j=1}^{l_o} \omega_{kj} f_1 \left( \sum_{i=1}^{n} V_{ji}p_i + b_{jo} \right) + b_{ko} \right) \\
L_gL_f h(x) &= f_2 \left( \sum_{j=1}^{l_o} \omega_{kj} f_1 \left( \sum_{i=1}^{n} V_{ji}p_i + b_{jo} \right) + b_{ko} \right)
\end{align*}$$

(28)

For two layer the FFNN, as shown in Fig. 6, consider $l_o$ and $k_1$ are the number of neurons in layer1 and layer2, respectively. So, the above equations can also be presented in the vectors form as

$$L^2_J h(x) \text{ or } L_gL_f h(x) = \tilde{f}(\tilde{W}^T \tilde{f}(\tilde{V}^T \tilde{p} + b_v) + b_w)$$

(29)

More explicitly, this expression can be expressed as follows

$$L^2_J h(x) \text{ or } L_gL_f h(x) = (\text{tanh}(\tilde{V}^T \tilde{p} + b) + b_v)$$

(30)

After selection of the network structure, the network training is done by minimizing the cost function. The cost function is generally characterized as follows

$$J(V_{ji}, \omega_{kj}) = \frac{1}{2} \sum_{i=1}^{l_o} (t_k - z_k)^2$$

(31)

where $t_k$ is the target output at the $k^{th}$ output node and $J(V_{ji}, \omega_{kj})$ is the mean square error (MSE).

Levenberg-Marquardt training algorithm is used for updating the weights of the FFNN. The MSE criterion or the maximum number of iterations decide the termination of the iterative process. A range of values of the network parameters has been varied systematically to achieve a good estimate of the training data. The varying network parameters are the number of hidden neurons in the hidden layers, with learning rate range and the number of iterations are used for the estimation of $L^2_J h(x)$ and $L_gL_f h(x)$.

The final FFNN structure for $L^2_J h(x)$ and $L_gL_f h(x)$ has three layer and the learning rate is 0.1. The first layer consists of the inputs. The second layer which is the hidden layer consists of ten neurons with sigmoid function as an activation function. The third layer is an output layer which gives us

\[\text{Characteristics curves of } C_p \text{ by varying } \beta.\]

\[\text{FFNN for } L^2_J h(x) \text{ and } L_gL_f h(x) \text{ generation.}\]
$L_2^2 h(x)$ and $L_2 L_f h(x)$ as an estimates of the plant drift terms and input channel, respectively. This choice of the network parameters yields a good match between the actual and the predicted values.

![FIGURE 7. Performance plot.](image)

1) SIMULATION RESULTS OF FFNN
The performance in terms of MSE, during the estimation of $L_2^2 h(x)$ and $L_2 L_f h(x)$, is shown in Fig. 7. It the start there is considerable amount of error. However, with the increase in epoches, the error reduces to its minimum value. Their regression plots, depicted in Fig. 8, are plotted against the target values. The regression parameter $R$ decides the success rate of estimation. If $R = 1$, it mean good estimates are made and as $R$ decreases the true estimation decreases.

![FIGURE 8. Regression plot.](image)

The estimation error histogram associated with $L_2^2 h(x)$ and $L_2 L_f h(x)$ shown in Fig. 9. It reveals a very small error with an average very close to zero.

![FIGURE 9. Mean squared error histogram.](image)

This estimation provides the estimates ($L_2^2 h(x)$ and $L_2 L_f h(x)$) which will be used in control algorithm outlined in next section.

V. GENERALIZED GLOBAL SLIDING MODE CONTROL
In this section the GGSFC based control law is designed to extract maximum power from the WECS. This job can be done by steering $\omega_h$ to $\omega_{opt}$ by logically varying the control input $u$ (i.e., $R_1$). Now, by considering the output based normal form (20) subject to uncertainties. Thus one may have

$$
\begin{align*}
\dot{z}_1 &= z_2 \\
\dot{z}_2 &= L_2^2 h(x) + L_2 L_f h(x)u + \Delta(z_1, z_2, t)
\end{align*}
$$

where $z_1 = x_3$ and $z_2 = \frac{1}{2}(d_1 y_1^2 + d_2 y_3 + d_3 x_2^2 - p\phi_m x_2)$ and $\Delta(z_1, z_2, t)$ is the uncertainty which is assumed to be matched and bounded by a positive constant $K$ i.e., $|\Delta(z_1, z_2, t)| \leq K$.

Since the ultimate objective is the tracking of the optimum speed of the generator named as $\omega_{opt}$. Therefore, the mismatch between the actual and reference speed is defined by

$$
e = z_1 - \omega_{ref}
$$

where $\omega_{ref} = \omega_{opt}$. Based on this error, a new variable $\sigma$ is defined as follows

$$
\sigma = \dot{e} + ae - f(t)
$$

where the function $f(t)$, called the forcing function, must be designed (according to [45]) to meet the following three conditions so that $\sigma = 0$ is satisfied for all $t \geq 0$.

1) $f(0) = \dot{e}_0 + ae_0$
2) $f(t) \to 0$ as $t \to \infty$
3) $f(t)$ has a bounded first time derivative

Here $\dot{e}_0$ and $e_0$ are the velocity and position errors respectively, at $t = 0$. The detailed mathematical expression of $f(t)$ in GGSFC is chosen as follows

$$
f(t) = [(\dot{e}_0 + ae_0)\cos bt - be_0\sin bt]\exp(-at)
$$
where \(a\) and \(b\) are positive constants. Note that, this forcing function satisfy all the above three conditions.

When \(\sigma = 0\) is met, then the solution of the closed loop system will be governed by the following differential equation \(\dot{e} + ae - f(t) = 0\). The solution of this equation appears as follows

\[
e(t) = (e_0 \cos bt + \frac{\dot{e}_0 + ace_0}{b} \sin bt) \exp(-at) \tag{36}\]

It is worthy to mention that this solution can also be obtained by solving the forthcoming second order system

\[
\ddot{e} + 2a\dot{e} + (a^2 + b^2)e = 0 \tag{37}
\]

with initial conditions \(\dot{e}(0) = \dot{e}_0\) and \(e(0) = e_0\).

The poles of this system are lying at \(-a \pm bj\). This gives the indication that the dynamics of the system, in sliding mode, does not reduces which implies that the system experiences integral sliding mode for all \(t \geq 0\).

The time derivative of (34) along system (32) becomes

\[
\dot{\sigma} = z_2 - \hat{\omega}_{\text{opt}} + c(\dot{z}_1 - \hat{\omega}_{\text{opt}}) - f(t) \tag{38}\]

At this stage, the main interest is that the system should evolves with full states. Thus, a proportional integral surface in term of \(\sigma\) can be defined as follows

\[
\xi = \sigma + e \int_0^t \sigma(\tau)d\tau \tag{39}\]

The choice of such proportional integral surface carries very interesting meaning. This is actually a PI type manifold which provides us no order reduction (to the order of system’s dynamics) in sliding mode. Consequently, the system evolves with full states in sliding mode from the very start which results in enhanced robustness. In addition, this type of surface accompanied by the strong reachability law (reported in equation (43)) results in the suppressed chattering phenomenon.

The time derivative of \(\xi\) becomes

\[
\dot{\xi} = \dot{\sigma} + c\dot{\sigma} \tag{40}\]

Now incorporating the values of \(\sigma\) and \(\dot{\sigma}\) and then posing \(\ddot{\xi} = 0\) and then calculating for the input \(u\), one may get

\[
u_{\text{equ}} = \frac{1}{kg_fh}[-a(z_2 - \hat{\omega}_{\text{opt}}) - i^2f h + \hat{\omega}_{\text{opt}} + f(t)] \tag{41}\]

Since the practical system always operates under uncertainties therefore, the equivalent control alone will be no more capable to enforce sliding mode. So, the overall sliding mode enforcement law appear as follows

\[
u = u_{\text{equ}} + u_{\text{dis}} \tag{42}\]

where

\[
u_{\text{dis}} = -k_1(\xi + W\text{sign}(\xi)); \quad 0 < W < 1. \tag{43}\]

The schematic diagram of the designed control technique is shown in Fig. 10.

**Theorem 1:** The sliding mode will be enforced along the manifold (39) by the control law of the (43) and hence the tracking will happen if the switching gain of the discontinuous control component (i.e., \(u_{\text{dis}}\)) chosen larger than the bound of the uncertainty i.e.,

\[
K > |\Delta(z_1, z_2, t)| + \eta \tag{44}\]

**Proof:** Now, at this stage we are ready to confirm sliding mode establishment. A lyapunove function, in term of the sliding variable, is defined as follows.

\[
V = \frac{1}{2}\dot{\xi}^2 \tag{45}\]

The time derivative of this function along (41) becomes

\[
\dot{V} = \dot{\xi}\dot{\xi} = \xi(\dot{\sigma} + c\dot{\sigma}) \tag{46}\]

Using (38) and (42) (with components given in (41) and (43)), one may get

\[
\dot{V} = \xi(-k_1(\xi + W\text{sign}(\xi)) + \Delta) \tag{47}\]

This expression remains true, i.e., negative definite, if

\[
k_1W - |\Delta| \geq \eta > 0 \tag{48}\]

The inequality (47) can also be written as

\[
\dot{V} \leq -k_1\dot{\xi}^2 - k_1W|\xi| + |\xi||\Delta| \tag{49}\]

or

\[
\dot{V} \leq -k_1\dot{\xi}^2 - |\xi|(k_1W - |\Delta|) \tag{50}\]

The differential inequality is a fast finite time converging equation, which confirms that \(V\) approaches to zero in finite time. It means that \(\dot{\xi}\) approaches to zero. As \(\dot{\xi} \rightarrow 0\), the equation (40) becomes

\[
\dot{\sigma} + c\dot{\sigma} = 0 \tag{51}\]

The homogeneous equation has a solution

\[
\sigma(t) = \sigma(0)\exp(-at) \tag{52}\]
It means that \( \sigma \) will approach to zero. The \( \sigma \) convergence to zero certify the equation (37) with solution reported in (36). Thus, the tracking error converges to zero which in turn provide us the reference tracking. This proves the theorem. Having tracked the reference, the maximum power will be extracted via the equation (1).

VI. SIMULATION RESULTS AND DISCUSSIONS
In this section, the closed loop simulation results of the afore said process are displayed. In the first subsection the robust tracking performance in an uncertain scenario is performed while in the second subsection the comparison to standard literature results is shown.

![FIGURE 11. Wind speed profile.](image)

<table>
<thead>
<tr>
<th>TABLE 2. Parameters of wind turbine.</th>
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<tbody>
<tr>
<td>Parameter</td>
</tr>
<tr>
<td>Air density ( \rho )</td>
</tr>
<tr>
<td>Blade radius ( R_b )</td>
</tr>
<tr>
<td>Maximum power coefficient ( C_p )</td>
</tr>
<tr>
<td>The tip speed ratio ( \lambda ) (optimum value)</td>
</tr>
</tbody>
</table>

A. ROBUST TRACKING PERFORMANCE
The VS-WECS equipped with PMSG has been build based on equations (1) to (16). The power rating of the VS-WECS equipped with PMSG is 3 kilo Watt (kW). The wind speed profile is generated through Kaimal spectra is shown in Fig. 11 reported in [46]. The simulations has been performed using variable step ode45 solver. Different parameters of the wind turbine and PMSG are shown in table 2 and table 3 of Appendix, respectively. These parameters are adapted from [37]. In order to verify the tracking performances of the investigated controller, the simulation results are shown in Fig. 12-14. In Fig. 12, the tracking performance of the reference generator speed by the actual speed of the generator is ensured by GGSMC. In Fig. 13 and Fig. 14, power coefficient \( C_p \) and the tip speed ratio \( \lambda \) are displayed, respectively. The actual variations in \( C_p \) and \( \lambda \) can be seen in the zoomed sections of the Fig. 13 and 14. The \( C_p \) value was found very close to its optimum value of 0.47 where as the \( \lambda \) was found very closed to its optimum value 7.

![FIGURE 12. Reference speed tracking via shaft speed.](image)

![FIGURE 13. Power coefficient evolution.](image)

![FIGURE 14. Tip speed ratio vs time.](image)

It is important to mentioned that the wind speed tracking was performed in uncertain scenarios. The uncertainties of matched kind were \( 0.5 \sin(t) \) while the plant parameters were varied with a change of 5%. The performance is quit good.
and the maximum power is nicely extracted by keeping the power coefficient $C_p$ and the tip speed ratio $\lambda$ close to their optimum values. Hence the NNs base GGSMC displays its self as an appealing candidate for such power systems.

**FIGURE 15.** GGSMC tracking performance in comparison with results of [37].

**FIGURE 16.** Comparison of power coefficient $C_p$.

**FIGURE 17.** Comparison of tip speed ratio $\lambda$.

**B. COMPARISON WITH STANDARD LITERATURE RESULTS**

To highlight the performance of the NNs based GGSMC, its results are compared with the feedback linearized controller [37]. The tracking performance of both the controllers, in the fast transients, are also shown in zoomed views in the Figure. The power coefficient has its optimum value near to 0.47 which is ensured the best by GGSMC with no oscillations as compared to feedback linearized controller (one may see then in Fig. 16). The GGSMC have tip speed ratio almost around optimal tip speed ratio as compared to feedback linearized controller, as shown in Fig. 17, which guarantees maximum power extraction from the wind at the given wind speed.

Hearing observed the comparative results, its very clear that the FFNN based GGSMC proves its self an appealing candidate for MPPT designs in wind power systems.

**VII. CONCLUSION**

In this paper NNs based GGSMC MPPT law have been investigated for a variable wind speed turbine which is connected a PMSG. The unknown nonlinear dynamics (i.e., drift terms and input channels) are estimated via the FFNN and a robust GGSMC law is developed which maintain the $C_p$ and $\lambda$ at it required values and confirms maximum power extraction. The sliding mode enforcement stability is also presented in details. To highlight the benefits of the FFNN based GGSMC, its results are compared with standard literature results (i.e., feedback linearized controllers [37]). At the end it is confirmed that the newly investigated FFNN base GGSMC is an appealing candidate for such tasks in power systems.

**APPENDIX**

See Tables 2 and 3.

**REFERENCES**


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