

Technologies and
Mathematical Modeling of
Fines-Assisted Oil and Gas Recovery

Abbas Zeinijahromi, B.Sc.(Hons), M.Sc.

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Australian School of Petroleum
Faculty of Engineering, Computer & Mathematical Sciences
The University of Adelaide



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Table of Contents

Abstract	iii
Statement of Originality	v
Acknowledgment	vi
Thesis by Publication	viii
Statement of Authors' Contributions	x
1 Contextual Statement	1
1.1 Thesis Structure	4
1.2 How the Publications Are Related to This Thesis	7
1.3 References	10
2 Literature Review	13
2.1 Introduction	13
2.2 Suspension Transport in Porous Media	14
2.2.1 <i>Surface Interactions</i>	15
2.2.2 <i>Hydrodynamic Forces</i>	20
2.2.3 <i>Classical Filtration Theory</i>	21
2.3 Low Salinity Water-Flooding as an Improved Oil Recovery Technique ..	25
2.4 References	29
3 Maximum Retention Concentration Function as a Model for Particles Detachment in Porous Media	33
3.1 Particle Detachment under Velocity Alternation during Suspension Transport in Porous Media	34
3.2 Well Impairment by Fines Migration in Gas Fields	60
3.3 Effects of Fines Migration on Well Productivity during Steady State Production.....	72
3.4 Skin due to Fines Mobilization, Migration, and Straining during Steady State Oil Production.....	88

4 Analytical Model for Fines-Assisted Water-flood in Quasi 2-D Layer-Cake Formations.....	98
4.1 Effects of Induced Fines Migration on Water Cut during Waterflooding.....	99
4.2 Effects of Injected-Water Salinity on Waterflood Sweep Efficiency through Induced Fines Migration	109
5 Two-Phase Flow in Natural Rocks with Fines Lifting, Migration, and Straining.....	123
5.1 Improved Oil Recovery by Mobilizing Fines during Waterflooding (Laboratory-Based Incremental Recovery)	124
6 Modeling and Applications of Low Salinity Fines-Assisted Water-flooding (New Improved Oil Recovery Method).....	141
6.1 Mathematical Model for Fines Migration Assisted Waterflooding with Induced Formation Damage	142
6.2 Fines Migration Assisted Improved Gas Recovery during Gas Field Depletion.....	172
7 Conclusions.....	195

Abstract

This is a PhD thesis by publication. It includes seven published/accepted for publication journal papers and two submitted papers in academic peer reviewed journals. The content of the thesis is also published in ten full volume technical papers of Society of Petroleum Engineering (SPE).

The thesis develops a theory for single and two-phase flow in porous media accounting for mobilization, migration, and straining of the natural reservoir fines. This phenomenon has been widely reported in laboratory studies and also well history data. The existing mathematical model, widely used in petroleum reservoir simulation, does not agree with laboratory observations. It contains phenomenological empirical constants which cannot be predicted theoretically.

The new closed system of governing equations, proposed in the current thesis, is free of the above mentioned shortcomings. The proposed system contains a new theoretical function describing the rock capacity to liberate fines so-called maximum retention function. This function is based on the micro scale conditions of mechanical equilibrium of fine particles in the porous space. The mechanical equilibrium condition is a torque balance of drag, lifting, electrostatic, gravity, and capillary forces. The maximum retention function is derived for both single-phase and two-phase flows in porous media. The comparison between the modified particle detachment model and the maximum retention function and laboratory and well data has shown a good agreement, which validates the model.

An exact analytical solution for single-phase flow in porous media with alternating velocity accounting for fines lifting has been derived, allowing for

mathematical description of a laboratory test on the suspension injection into reservoir cores with alternating velocities. Good agreement between the laboratory test results and the mathematical modeling predictions validates the theory developed.

Both analytical and numerical models for two-phase flow with induced fines migration have been developed. In reservoir scale approximation, the equivalence between the fines assisted water-flood and adsorption-free polymer flood has been investigated. It allows using the existing commercial simulators to model low salinity water-flood. The results of the modeling allow proposing a new technologically effective and economical method for improved sweep efficiency by fines assisted water-flooding.

Moreover, modeling of low salinity water injection shows that permeability reduction due to induced fines migration can slow down the encroaching water in oil/gas reservoir under strong water support. It decreases water production during pressure depletion of oil/gas reservoirs and improves the recovery. Also, a small volume injection of low salinity water can be used to reduce the water conning problem in oil/gas wells and prolong the wells production life.

Statement of Originality

This work contains no material which has been accepted for the award of any other degree or diploma in any university or other tertiary institution to Abbas Zeinijahromi and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text.

I give consent to this copy of my thesis when deposited in the University Library, being made available for loan and photocopying, subject to the provisions of the Copyright Act 1968.

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Abbas Zeinijahromi

21/08/2012

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Thesis by Publication

Published Journal Papers

Bedrikovetsky, P., **Zeinijahromi, A.**, Siqueira, F., Furtado, C. and de Souza, A., 2012. Particle Detachment Under Velocity Alternation During Suspension Transport in Porous Media. *Transport in Porous Media*, 91(1): 173-197.

Zeinijahromi, A., Lemon, P. and Bedrikovetsky, P., 2011. Effects of Induced Migration of Fines on Water Cut during Waterflooding. *Journal of Petroleum Science and Engineering*, 78: 609-617.

Zeinijahromi, A., Vaz A., Bedrikovetsky, P., 2012, Well impairment by fines migration in gas fields. *Journal of Petroleum Science and Engineering*, 88–89:125–135.

Zeinijahromi, A., Vaz A., Bedrikovetsky, P., Borazjani, S. 2012. Effects of Fines Migration on Well Productivity during Steady State Production. *Journal of Porous Media*. 15(7): 665-679.

Lemon, P., **Zeinijahromi, A.**, Bedrikovetsky, P. and Shahin, I., 2011. Effects of Injected-Water Salinity on Waterflood Sweep Efficiency through Induced Fines Migration. *Journal of Canadian Petroleum Technology*, 50(9): 82-94.

Bedrikovetsky, P., Vaz A., Machado F., **Zeinijahromi, A.**, Borazjani, S. 2012. Skin due to Fines Mobilisation, Migration, and Straining during Steady State Oil Production. *Journal of Petroleum Science and Technology*, 30:1539-1547.

Papers Accepted for Publication

Zeinijahromi, A., Nguyen T. K. P, Bedrikovetsky, P. accepted for publication 06/2012. Mathematical Model for Fines Migration Assisted Waterflooding with Induced Formation Damage, *SPE Journal*.

Submitted Journal Papers

Hussain, F., **Zeinjahromi, A.**, Bedrikovetsky, P., Cinar, Y., Badalyan, A., Carageorgos, T. submitted 04/2012. Improved Oil Recovery by Mobilizing Fines during Waterflooding (Laboratory-Based Incremental Recovery). *Journal of Canadian Petroleum Technology*.

Nguyen T. K. P., **Zeinjahromi A.**, Bedrikovetsky, P. submitted 08/2011. Fines migration assisted improved gas recovery during gas field depletion. *Journal of Petroleum Science and Engineering*.

Statement of Authors' Contributions

This thesis comprises a portfolio of nine publications that have been published, accepted for publication and/or submitted for publications in accordance with 'Academic Program Rules and Specifications 2012'. All journals to which the papers have been submitted are indexed in the 'ERA 2012 Journal List' database. The research summarized in the papers that constitute this thesis was undertaken within 'Formation Damage and EOR Research Group' at Australian School of Petroleum and with other universities and industry collaborators. Hence all the papers presented herein are co-authored and detail statements of relative contributions are endorsed by the co-authors.

STATEMENT OF AUTHORSHIP

Particle Detachment under Velocity Alternation during Suspension Transport in Porous Media

P. Bedrikovetsky, A. Zeinijahromi, F. Siqueira, C. Furtado, A. de Souza
Transport Porous Media, 2012, 91(1), 173-197

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Derivation of the exact solution, numerical calculations, comparative study between test and model data, participating in writing the text and formulating the final conclusions

Certification that the statement of contribution is accurate

SignedDate.....

F. Siqueira

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Development of analytical model, mathematical numerical modelling, sensitivity study

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

Date **04 Jun 2012**

C. Furtado

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Carrying out the laboratory tests

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

.....Date **June, 11th 2012**

A. de Souza

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Formulation of the problem

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 06/04/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Development of basic equations, writing the manuscript, acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed .. Date 12/06/2012

STATEMENT OF AUTHORSHIP

Well impairment by fines production in gas fields

A. Zeinjahromi, A. Vaz, P. Bedrikovetsky

Journal of Petroleum Science and Engineering, 2012

A. Zeinjahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Derivation of the exact solution, numerical calculations, comparative study between test and model data, participating in writing the text

Certification that the statement of contribution is accurate

SignedDate.....

A. Vaz,

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Literature review, Formulation of the problem, Discussion of the results

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis.

SignedDate *06/24/2012*.....

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation, manuscript evaluation, and acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate *12/06/2012*.....

STATEMENT OF AUTHORSHIP

Effects of Fines Migration on Well Productivity during Steady State Production

A. Zeinijahromi, A. Vaz, P. Bedrikovetsky, S. Borazjani

Journal of Porous Media, 2012, 15 (7): 665–679

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Derivation of the exact solution, numerical calculations, comparative study between test and model data, participating in writing the text

Certification that the statement of contribution is accurate

Signed Date

A. Vaz,

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performing literature review, Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date ... *Ok. 10/4/2012*

S. Borazjani

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date .. *06/04/2012*

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation, manuscript evaluation and acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

.....Date.....12/06/2012

STATEMENT OF AUTHORSHIP

Skin due to Fines Mobilisation, Migration and Straining during Steady State Oil Production

P. Bedrikovetsky, A. Vaz, F. Machado, A. Zeinijahromi, S. Borazjani

Journal of Petroleum Science and Technology: accepted for publication 12/2011

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performed analysis, interpreted data and wrote manuscript

Certification that the statement of contribution is accurate

SignedDate.....

A. Vaz,

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performing literature review. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate...06/04/2012

F. Machado

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate...06/04/2012

S. Borazjani

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Numerical modelling. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date ... 06/04/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation, manuscript evaluation and acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 12/06/2012

STATEMENT OF AUTHORSHIP

Effects of induced fines migration on water cut during waterflooding

A. Zeinijahromi, P. Lemon, P. Bedrikovetsky

Journal of Petroleum Science and Engineering, 2011, 78, 609-617

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Derivation of the exact solution, numerical calculations, comparative study between test and model data, participating in writing the text

Certification that the statement of contribution is accurate

SignedDate.....

P. Lemon

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performed the literature review. Contributed to planning of article and provided critical evaluation, participating in writing the text

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate 11/5/12.....

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation and manuscript evaluation and acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate 12/06/2012.....

STATEMENT OF AUTHORSHIP

Effects of Injected -Water Salinity on Waterflood Sweep Efficiency Through Induced

P. Lemon, A. Zeinijahromi , P. Bedrikovetsky, I. Shahin

Journal of Canadian Petroleum Technology, 2011, 50(9), 82-94

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

performed detailed analysis on all samples, interpreted data and participating in writing the text

Certification that the statement of contribution is accurate

Signed Date.....

P. Lemon

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Contributed to planning of article and provided critical evaluation, participating in writing the text, and formulating the final conclusions, performed literature review and conceptual analysis

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 13/6/2012

I. Shahin

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Contributed to planning of article and provided critical evaluation, performed literature review and conceptual analysis

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 13/6/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation, manuscript evaluation and acted as corresponding author

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

.....Date..... 12/06/2012

STATEMENT OF AUTHORSHIP

Improved Oil Recovery with Waterflooding by Mobilising Fines (laboratory-based incremental recovery)

F. Hussain, A. Zeinijahromi, P. Bedrikovetsky, Y. Cinar, A. Badalyan, T. Carageorgos
Journal of Canadian Petroleum Technology, 2012 : submitted paper

A. Zeinijahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Derivation of the exact solution, numerical calculations, comparative study between test and model data, participating in writing the text, formulating the final conclusions, and acted as corresponding author

Certification that the statement of contribution is accurate

SignedDate.....

F. Hussain

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Carried out main laboratory study. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate... 04/06/2012

Y. Cinar

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Carried out laboratory study. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate..... 4/6/12

A. Badalyan

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Carried out laboratory study. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

.....Date 06.06.2012

T. Carageorgos

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Carried out laboratory study. Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed .

.....Date 07/06/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation and manuscript evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed

.....Date 12/06/2012

STATEMENT OF AUTHORSHIP

Mathematical Model for Fines Migration Assisted Waterflooding with Induced Formation Damage

A. Zeinjahromi, T. K. P Nguyen, P. Bedrikovetsky

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A. Zeinjahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performed analysis, interpreted data, wrote manuscript and acted as corresponding author

Certification that the statement of contribution is accurate

Signed Date

T. K. P Nguyen

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 12/06/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation and manuscript evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

Signed Date 12/06/2012

STATEMENT OF AUTHORSHIP

Fines migration assisted improved gas recovery during gas field depletion

T. K. P Nguyen, A. Zeinjahromi, P. Bedrikovetsky

Journal of Petroleum Science and Technology, 2011: submitted paper

A. Zeinjahromi (Candidate)

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performed analysis on all samples, interpreted data, wrote manuscript and acted as corresponding author

Certification that the statement of contribution is accurate

SignedDate.....

T. K. P Nguyen

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Performed numerical reservoir modelling. Performed analysis of calculation results.

Contributed to planning of article and provided critical evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate...04/06/2012

P. Bedrikovetsky

Statement of contribution (in terms of the conceptualization of the work, its realization and its documentation)

Supervised development of work, helped in data interpretation and manuscript evaluation

Certification that the statement of contribution is accurate and permission is given for the inclusion of the paper in the thesis

SignedDate...12/06/2012