

NICOLAS IVANCEVIC

TOWARDS RENORMALIZABLE GRAVITY  
WITHOUT NEGATIVE-ENERGY STATES

November 19, 2013

*The Department of Physics, University of Adelaide*



*I certify that this work contains no material which has been accepted for the award of any other degree or diploma in my name, in any university or other tertiary institution and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text. In addition, I certify that no part of this work will, in the future, be used in a submission in my name, for any other degree or diploma in any university or other tertiary institution without the prior approval of the University of Adelaide and where applicable, any partner institution responsible for the joint-award of this degree.*

*I give consent to this copy of my thesis, when deposited in the University Library, being made available for loan and photocopying, subject to the provisions of the Copyright Act 1968.*

*The author acknowledges that copyright of published works contained within this thesis resides with the copyright holder(s) of those works.*

*I also give permission for the digital version of my thesis to be made available on the web, via the University's digital research repository, the Library Search and also through web search engines, unless permission has been granted by the University to restrict access for a period of time.*



I would like to thank my supervisors R. J. Crewther and M. A. Lohe for the patience and support that they have demonstrated throughout my candidature.



# Towards renormalizable gravity without negative-energy states

Nicolas Ivancevic

*Special Research Centre for the Subatomic Structure of Matter and  
The Department of Physics, University of Adelaide, Adelaide SA 5005, Australia*

(Dated: November 19, 2013)

A second-derivative gauge theory with a massless spin-2 boson on flat spacetime is presented. The dynamical symmetry preserves the spacetime metric and follows from an alternative interpretation of the equivalence principle. Gauge ambiguity is eliminated by a choice of reference frame, and the gauge boson propagator is derived from an invariant four-parameter polynomial action involving only dimensionless couplings. It is deduced that the theory is power-counting renormalizable in this gauge for almost all configurations of parameters. Examination of the linearized radiation then shows that, for some of these configurations, all excitations have non-negative canonical energy density. The paper concludes with an analysis of the static isotropic solutions to the weak-field vacuum equations.

## CONTENTS

I. Introduction .....	1
II. Dynamical symmetry .....	3
III. Gauge covariance.....	6
IV. Invariant action .....	8
V. Aspects of quantization .....	11
VI. Propagator.....	13
VII. Plane waves.....	16
VIII. Weak-field potential.....	18
IX. Test particle trajectories.....	19
X. Conclusion .....	24
Acknowledgments.....	25
A. Chiral representation.....	25
B. Spherical coordinates .....	27
References .....	27

## I. INTRODUCTION

To conceive a consistent quantum theory compatible with observable gravitational phenomena is widely recognized as an outstanding challenge of theoretical physics. Unfortunately, applications of established quantum field theory techniques to general relativity fall short due to the form of the implied interactions. Their negative mass dimensionality suggests that ultraviolet divergences cannot be removed by renormalization of a finite number of parameters.

It so happens that pure gravity, as dictated by Einstein's theory, is finite at one loop [1] due to a cancellation particular to four spacetime dimensions. However, coupling to matter—whether it be of scalar [1], Maxwell [2], Yang-Mills [3], or Dirac [4] type—introduces nonrenormalizable divergences at that same order. And even pure gravity diverges at two loops [5].

Recent approaches to the subject involve (a) more general quantization procedures, often with perturbative notions discarded, or (b) exotic frameworks such as string theories. In many cases, one must relinquish ideas from conventional gauge theories