

# A Generic Mechanics Approach for Predicting Shear Strength of Reinforced Concrete Beams

by

Tao Zhang

Thesis submitted for the degree of Doctor  
of Philosophy at The University of  
Adelaide  
(The School of Civil, Environmental and  
Mining Engineering)  
Australia

- December 2014 -

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## ABSTRACT

This thesis includes a series of journal articles in which a mechanics based segmental approach is developed for simulating shear behaviour of reinforced concrete (RC) beams. Using the well-established theories of partial interaction and shear friction, the generic mechanics approach simulates the formation and widening of diagonal cracks and shear sliding failure for RC beams. Being mechanics based, the proposed approach can be generally applied to various kinds of structures, that is any cross section, with any type of concrete and reinforcement and with any bond properties. Moreover, no component of the proposed approach relies on empiricism to account for the mechanics of shear failure, and the approach can accommodate any material characteristics which with time can be refined and revisited to improve the accuracy of shear strength simulation.

In developing the mechanics of the segmental approach for prestressed RC beams, it is shown how the approach is applied to analyse shear behaviour and simulate shear failure of prestressed beams. Parametric studies are conducted to explain the effect of prestress on shear behaviour. For verification, the proposed approach is applied to 102 specimens and the analytical and experimental results are in good agreement.

The generic nature of the mechanics approach is shown by its application to steel and fibre-reinforced polymer (FRP) reinforced beams and one-way slabs without stirrups. From the mechanics of the segmental approach, closed form solutions are derived for shear design and validated by comparisons with test results and code predictions of 626 steel and 209 FRP reinforced specimens.

Having developed closed form solutions for beams without stirrup, the approach is extended to incorporate shear reinforcement. Significantly, the partial interaction analyses of longitudinal and transverse reinforcements are directly linked. Furthermore, simple solutions are derived through mechanics for tension stiffening and can be applied for shear and flexure analysis in the segmental approach. The numerical and closed form solutions are applied to 194 specimens and validated with good correlation of predicted and measured results.

The generic mechanics approach is further extended to accommodate the effect of axial load on shear strength. The proposed approaches are applied to 61 specimens and simulation results show good agreement with test data.

A series of push-off tests are conducted to investigate the shear friction parameters for initially uncracked concrete under low levels of confinement. In addition, it is shown that the concrete shear friction properties can be extracted from simple confined cylinder tests and then applied in the segmental approach to predict shear sliding capacity. Thus this research highlights the potential to reduce the significant cost of empiricisms in terms of time and money when developing innovative RC products and generic design guidelines.

The broad application of the mechanics based segmental approach presents a general solution to simulate shear strength of RC beams. Thus the generic mechanics approach is a good extension of traditional shear analysis techniques as it obviates the necessity of empiricisms through huge amount of testings to determine shear strength of RC members.



## STATEMENT OF ORIGINALITY

I certify that this work contains no material which has been accepted for the award of any other degree or diploma in my name, in any university or other tertiary institution and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text. In addition, I certify that no part of this work will, in the future, be used in a submission in my name, for any other degree or diploma in any university or other tertiary institution without the prior approval of the University of Adelaide and where applicable, any partner institution responsible for the joint-award of this degree.

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Tao Zhang

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Date



# LIST OF PUBLICATIONS

## *Journal Papers*

- Oehlers, D. J., Visintin, P., Zhang, T., Chen, Y., and Knight, D. (2012). "Flexural rigidity of reinforced concrete members using a deformation based analysis." *Concrete in Australia*, 38(4), 50-56.
- Zhang, T., Visintin, P., Oehlers, D. J. and Griffith, M. C. (2014). "Presliding shear failure in prestressed RC beams. I: Partial-Interaction mechanism." *ASCE Journal of Structural Engineering*, 10.1061/(ASCE)ST.1943-541X.0000988, 04014069.
- Zhang, T., Visintin, P., Oehlers, D. J. and Griffith, M. C. (2014). "Presliding shear failure in prestressed RC beams. II: Behavior." *ASCE Journal of Structural Engineering*, 10.1061/(ASCE)ST.1943-541X.0000984, 04014070.
- Zhang, T., Visintin, P. and Oehlers, D. J. (2014). "Shear strength of steel RC beams and slabs without stirrups." Submitted to *ICE Structures and Buildings*.
- Zhang, T., Oehlers, D. J. and Visintin, P. (2014). "Shear strength of FRP RC beams and one-way slabs without stirrups." *ASCE Journal of Composites for Construction*, 10.1061/(ASCE)CC.1943-5614.0000469, 04014007.
- Zhang, T., Visintin, P. and Oehlers, D. J. (2014). "Partial-interaction tension-stiffening properties for numerical simulations." Submitted to *Structures*.
- Zhang, T., Visintin, P. and Oehlers, D. J. (2014). "Shear strength of RC beams with steel stirrups." Submitted to *ASCE Journal of Structural Engineering*.
- Zhang, T., Visintin, P. and Oehlers, D. J. (2014). "Shear strength of RC beams subjected to axial load." Submitted to *ASCE Journal of Structural Engineering*.
- Chen, Y., Zhang, T., Visintin, P., and Oehlers, D. J. (2014). "Concrete shear-friction material properties: application to shear capacity of RC beams of all sizes", Submitted to *Advances in Structural Engineering*.

## *Conference Paper*

- Zhang, T., Visintin, P., and Griffith, M. C. (2014). "A Unified Solution for Shear Design of FRP Reinforced Concrete Structures." *Proc., The 7th International Conference on FRP Composites in Civil Engineering*, CICE, Vancouver, Canada.



## **ACKNOWLEDGEMENTS**

My sincere gratitude goes first to Emeritus Prof. Deric Oehlers, who guided me through the ups and downs of the PhD study and led me into the wonderful palace of research. His excellent supervision, invaluable advice, continuous support and encouragement, were an enormous help to me in the completion of this work.

I would also like to thank Prof. Michael Griffith for his great guidance and patience throughout my studies, and Dr. Phillip Visintin for his prompt and precious suggestions and ideas whenever there was a problem in the research.

I am very thankful to laboratory staff, Mr. Ian Ogier, Mr. Jon Ayoub, Mr. Steven Huskinson, and Mr. Ian Cates, for their assistance with the experimental work. Special thanks are given to Mr. Ian Ogier for his support and cooperation, and impressive craftsmanship in the test configuration.

I also thank my colleague Yongjian Chen for his help in the experiment, and his collaboration and discussion in the research.

The financial support from the China Scholarship Council (CSC) and the University of Adelaide (UoA) are greatly appreciated.

Finally, to my parents and my partner, I am eternally grateful for their love, support, motivation, encouragement.